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Розроблено та досліджено чисельно-аналітичні моделі теплового нестационарного процесу та пов'язаної з ним похибки вимірювань волоконно-оптичних гіроскопів (ВОГ). З урахуванням значень температури, отриманих шляхом моделювання, а також результатів калібрування конкретних ВОГ, побудовано прогнози величин похибок вимірювань. Проведено порівняння результатів моделювання з експериментальними даними. Наведено рекомендації з розвитку результатів та їхнього практичного використання

Ключові слова: гіроскоп, скінченноелементна модель, нестационарна теплопровідність, інструментальні похибки, температурна модель, калібрування

Разработаны и исследованы численно-аналитические модели теплового нестационарного процесса и связанной с ним погрешности измерений волоконно-оптических гироскопов (ВОГ). С учетом значений температуры, полученных путем моделирования, а также результатов калибровки конкретных ВОГ, выполнен прогноз величин погрешностей измерений. Проведено сравнение результатов моделирования с экспериментальными данными. Приведены рекомендации по развитию результатов и их практическому использованию

Ключевые слова: гироскоп, конечно-элементная модель, нестационарная теплопроводность, инструментальные ошибки, температурная модель, калибровка

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ESTIMATION OF HEAT FIELD AND TEMPERATURE MODELS OF ERRORS IN FIBER-OPTIC GYROSCOPES USED IN AEROSPACE SYSTEMS

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1. Introduction

Fiber-optic gyroscopes (FOG) have been widely used recently in the control and navigation of aerospace systems [1]. Ensuring accuracy of measurement of external influenc-

es on instruments is an important technical problem. One of the main factors influencing FOG readings is the environment temperature variation. For the instruments installed aboard flying vehicles, this temperature can vary within a wide range. For example, temperature fluctuations can range

from $-120\text{ }^{\circ}\text{C}$ to $+120\text{ }^{\circ}\text{C}$ for an orbiting artificial earth satellite [2]. Under these circumstances, the design of on-board gyro systems requires application of special measurement simulation models taking into account the effect of temperature on the data accuracy. The matter of such model fidelity, both in terms of reproduction of thermal conditions and adequacy of the instrumental errors, is an open-ended question so far. In this regard, joint use of computational thermal-condition models and analytical instrumental-error models in which parametric setting is ensured by preliminary experimental studies is deemed to be promising. Parameters of the latter can be determined in the process of calibration of concrete FOG samples. Relevance of the work in this area is confirmed by the following: firstly, great attention is given recently to the issues of calibration and improvement of inertial system accuracy [3–5]; secondly, the demand for the study results on the part of Ukrainian space-rocket industry.

2. Literature review and problem statement

Both designing of new instruments and development of algorithms and software for processing results of measurements made with commercially available FOGs, are impossible without taking into account temperature effect on the instrument readings [6]. Consideration of such influence is done by analytical models having phenomenological character. Parameters of such models are determined experimentally during so-called calibration. Above models are generally used as compensating models directly in operation of measuring gyroscopic modules (MGM) [6–8]. This error compensation is done algorithmically, using appropriate mathematical software of the system containing MGM. For this purpose, temperature variation data coming from the inboard temperature sensor of FOG is used. The studies carried out by the authors of [9, 10] have shown that the influence of the temperature change rate on the FOG measurement accuracy is more significant than the temperature itself. Based on this, the temperature model of the FOG instrumental errors must include not only the measured temperature values but also assessment of its gradient, possibly in combination with the temperature value.

Recently published works are devoted to a direct determination of temperature fields in instruments, FOGs among them [6, 11]. Due to complexity of the instrument designs, use of a variety of materials in them and the need for a precise consideration of boundary conditions for numerical solution of boundary-value problems, the finite elements method (FEM) is applied. To solve the initially boundary problem of non-stationary thermal conduction, difference methods are also used [12]. The resulting values of numerical simulation of thermal fields in instruments give just a rough estimate of their thermal state. This is due to the fact that the calculation studies cannot always be successful in setting values of thermal-physic coefficients for various elements being the part of FOG. This information is not within everyone's reach.

In this connection, experimental studies of the heat distribution processes in instruments are of special importance. Comparison of experimental data with the results of numerical modeling enables to define more precisely source data for calculations. They help in creation of a refined model for numerous calculations of FOG thermal condition variants when designing control and navigation systems.

3. The research objective and tasks

The work objective is development of gyroscope measurement simulation methods close by their characteristics to real data under conditions of an extended instrument's operating temperature range and ensuring improved precision in functioning of platformless inertial navigation systems.

To achieve the objective, the following tasks were stated:

- carrying out thermal experiments with FOG to study temperature conditions of the instrument operation;
- development of a computational model of nonstationary thermal field in the FOG and its refinement using the experiment results;
- development of analytical models of temperature dependence of the FOG instrumental errors together with a procedure for experimental determination of their parameters;
- obtaining efficiency estimates of the developed methods for a concrete sample of FOG.

4. Experimental studies of thermal fields in fiber-optic gyroscopes

To perform thermal tests, an experimental stand was used. The stand included Acutronic heat chamber with appropriate measuring instrumentation [13]. The experiment objective was to obtain temperature dependence on time at given FOG and heat chamber points. In order to determine contribution of the incorporated Peltier element to the overall thermal state of the instrument, separate tests were conducted for operating (switched on) and nonoperating (switched off) FOG. Temperature was measured with DS18B20 sensors (USA) – digital thermometers of transistor (semiconductor) type with a programmable resolution. Preliminary calibration tests were conducted for 30 sensors of which 15 sensors were selected for experiments based on the results of statistical processing.

12 sensors were set on the FOG: 4 in the top cover, 4 in the bottom, and 4 in the side surfaces. Three sensors were installed in the chamber to control temperature of air flows: in two top corners and in one bottom corner (Fig. 1). Information from the sensors was recorded into a text file at specified intervals using analog-to-digital converter of the stand.

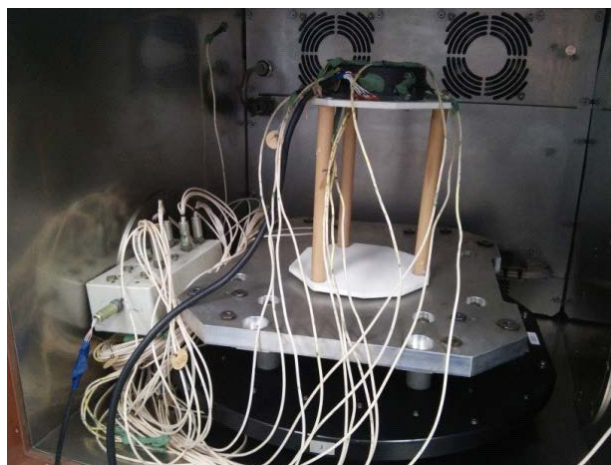


Fig. 1. FOG with sensors installed in the heat chamber

The program of heat flow variation in the chamber was taken for the tests. It is shown in Fig. 2 by the curve of temperature variation on the internal sensor of the stand when the FOG was in operating condition. This variation was provided thru exposure of the instrument at the initial temperature $T_0=30\text{ }^\circ\text{C}$, further temperature setting at $0\text{ }^\circ\text{C}$, holding at this temperature and a new temperature setting at $T_0=30\text{ }^\circ\text{C}$.

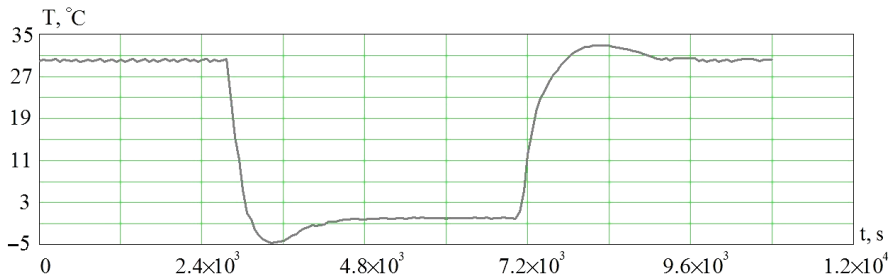


Fig. 2. Temperature ($T, \text{ }^\circ\text{C}$) vs. time ($t, \text{ s}$) graph obtained in testing the stand-alone FOG in the heat chamber

As a result of the cycle of tests of the working and non-working FOG, temperature dependence on time was obtained at the sensor location points. One of the important results is comparison of the temperature regimes on the body of the working and non-working instrument. Temperatures vs. time graphs are presented in Fig. 3 for the working (curve 1) and non-working (curve 2) gyroscopes. In this and the following graphs, time keeping was done from the moment of cooling. Analogous relationships with similar curve trend were obtained for the rest of sensors.

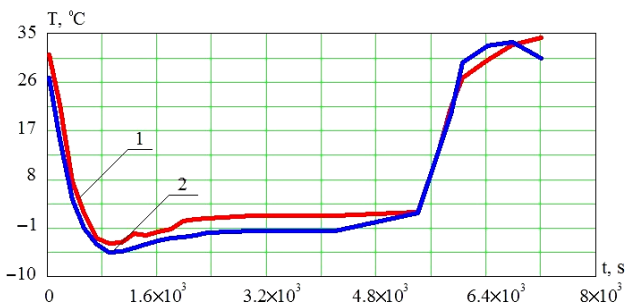


Fig. 3. Temperature ($T, \text{ }^\circ\text{C}$) vs. time ($t, \text{ s}$) graphs at the bottom point: 1 – for working FOG; 2 – for non-working FOG

Comparison of the curves in Fig. 3 shows that there are no fundamental distinctions in the temperature distribution depending on time. Action of the Peltier element exerts generally smoothing effect on the distributions. At rapid overheating or cooling, temperature changes proceed more smoothly to ensure regular FOG operating mode due to the work of this element.

5. Numerical modeling of thermal fields

For the numerical solution of the problems of nonstationary thermal conductivity of instrumentation, software package ANSYS Student 17.2 (USA) was used [14].

The problem of non-stationary thermal conduction was solved using the boundary condition of convective heat exchange [12] in which the ambient temperature was deter-

mined by means of internal sensor of the heat camera and 3 additional sensors installed for the experiment.

Following the analysis of the reference data and the results of the experiments conducted for finite element modeling, the following values of constants were accepted:

- 1) for the housing material (aluminum alloy):
 - density $\rho=2700\text{ kg/m}^3$;
 - specific heat $c=0.93\text{ J/kg }^\circ\text{C}$;
 - coefficient of thermal conductivity $k=140\text{ W/m}^\circ\text{C}$;
 - heat transfer coefficient $\alpha=60\text{ W/m}^2\text{ }^\circ\text{C}$;
- 2) for the coil material:
 - density $\rho=2200\text{ kg/m}^3$;
 - specific heat $c=920\text{ J/kg}^\circ\text{C}$;
 - coefficient of thermal conductivity $k=1.4\text{ W/m }^\circ\text{C}$;
 - heat transfer coefficient $\alpha=60\text{ W/m}^2\text{ }^\circ\text{C}$.

The coefficient of thermal conductivity of the optical fiber material wound on a coil is very small and equal to $1.4\text{ W/m}^\circ\text{C}$ (one hundred times smaller than the coefficient for the body material). This fact confirmed by numerical experiments permitted specification of conditions of absence of heat exchange (thermal insulation).for the surface of the FOG coil on which fiber is wound.

Thus, a simplified model was created for calculations. It consisted primarily of a housing, an internal coil on which optical fiber is wound and some elements disposed within the housing. The function of the heat source which simulates work of the Peltier element (it can provide both heating and cooling) and heat radiation from laser has been determined experimentally.

The FOG model (Fig. 4) was divided into 31882 tetrahedral finite elements. As an initial condition, uniform distribution of temperature $30\text{ }^\circ\text{C}$ corresponding to the start of the experiment has been taken.

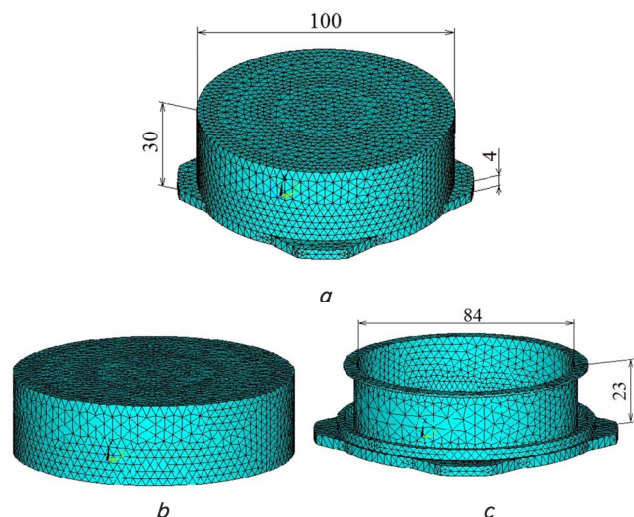


Fig. 4. Calculation model of FOG: a – complete; b – cover; c – FOG with the cover removed

The results of solution of the non-stationary conduction problem are shown in Fig. 5–9. Comparison of numerical and experimental results for all 12 measurement points has shown a quite satisfactory degree of their coincidence. As an

example, the temperature vs. time graphs for the top cover of the working (Fig. 5) and non-working (Fig. 6) FOG are given. In these figures, the calculated data are represented with the solid curve and the experimental data are represented with the curve with dots.

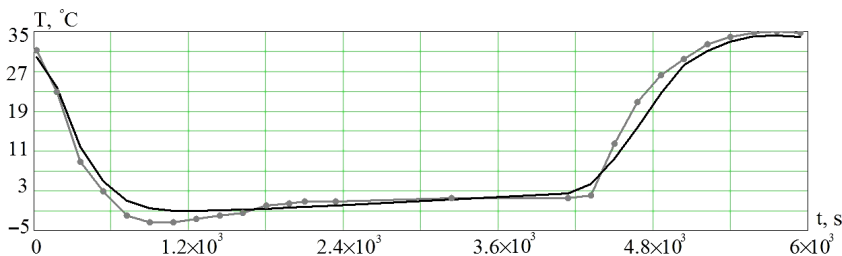


Fig. 5. Temperature ($T, ^\circ\text{C}$) vs. time (t, s) graphs for the top cover of the working FOG

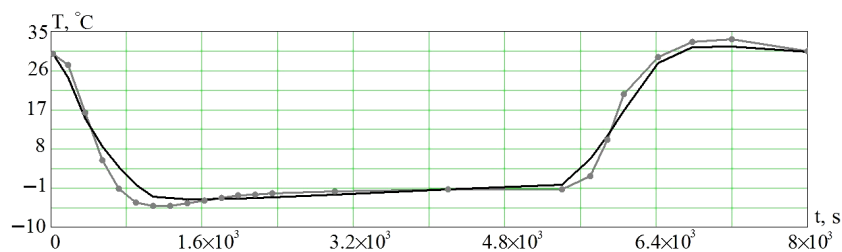


Fig. 6. Temperature ($T, ^\circ\text{C}$) vs. time (t, s) graphs for the top cover of the nonworking FOG

After processing the data obtained for the working instrument, it was established that dispersion D of experimental and numerical values was as follows: $D=4.256\text{ }^\circ\text{C}$ for the top surface; $D=1.807\text{ }^\circ\text{C}$ for the side surface and $D=9.143\text{ }^\circ\text{C}$ for the bottom.

The same magnitudes for the nonworking FOG were as follows: $D=4.764\text{ }^\circ\text{C}$ for the top surface; $D=3.348\text{ }^\circ\text{C}$ for the side surface and $D=6.361\text{ }^\circ\text{C}$ for the bottom.

The comparison of data and their quite satisfactory agreement obtained in this comparison have led to the conclusion that there is possibility of using this model in the calculation of the instrument thermal fields. Fig. 7–9 show some results.

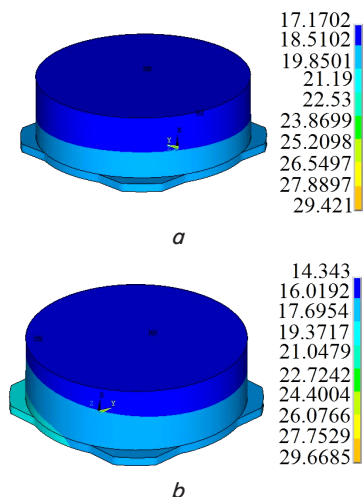


Fig. 7. Temperature distribution on the surface: a – for non-working instrument; b – for working instrument, $t=300\text{ s}$

As it might be expected, distributions were almost symmetrical (Fig. 7, a) for the non-working device. Comparison of the temperature distribution in the non-working and working instruments shown in Fig. 6 indicates that action of the Peltier element becomes evident already at the first stages of the cooling process: it is smoothing somewhat the impact of external heat variation leading to an asymmetric temperature field. Also, this effect is well illustrated in Fig. 8.

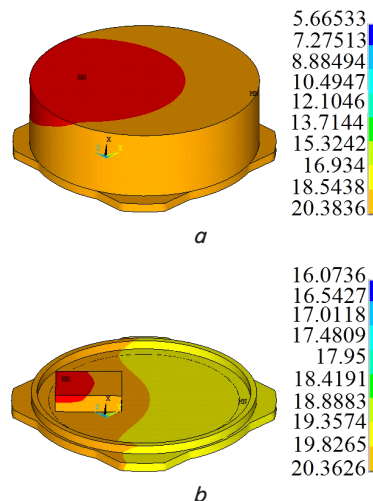


Fig. 8. Temperature distribution for the working instrument, $t=4800\text{ s}$: a – on the cover; b – with the cover removed

Fig. 9 shows the temperature vs. time graph obtained for the working instrument in one of the blocks of the finite element model corresponding to the location of the FOG's thermal sensor. This calculated temperature in conjunction with an estimate of its gradient is then used to determine temperature-dependent FOG's instrumental errors in the problem of simulation modeling of MGM operation at an arbitrarily assigned ambient temperature.

The numerical experiments and comparison of the obtained data with experimental ones show quite satisfactory qualitative and quantitative coincidence of the results. Consequently, the developed thermal model of FOG can be used for further analysis.

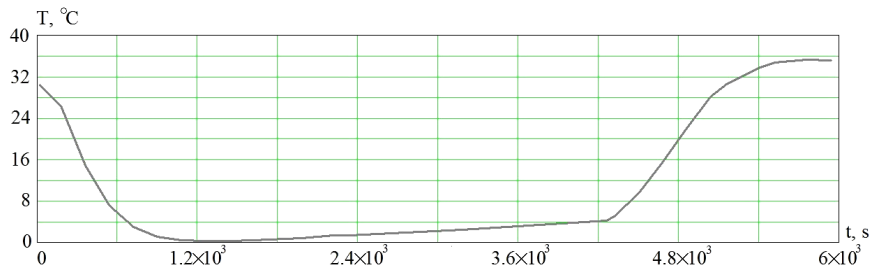


Fig. 9. The calculated temperature ($T, ^\circ\text{C}$) vs. time (t, s) graph for the working FOG at the point of location of the built-in temperature sensor

6. The model of FOG measurement errors and the method of determining its parameters

This section deals with the description of the mathematical relationship between the FOG measurements and

the value being measured taking into account instrumental errors (IE) of the instrument sensitive to the temperature factors. Parameters of this dependence (of the mathematical model) are determined from the experimental data obtained for the tested gyroscope samples through their approximation with analytical functions. Use of the experimental data provides model setup for a specific type of instruments. The resulting functional dependencies of IE are used in generating data from the measuring gyroscopic module (MGM) close by their characteristics to the real ones. Such measurements enable simulation of the gyroscopic system functioning throughout the operational temperature range. It is required in the design and research works.

Measurement model. Consider a measuring gyro module comprising three FOGs and introduce two systems of coordinate axes:

- X, Y, Z axes of the right orthogonal instrument coordinate system (RCS) connected with the MGM structure;
- axes coinciding with the FOG's sensitivity axes (SA) and close to the mutually orthogonal axes.

Let $\bar{\omega}_{MGM} = (\omega_x, \omega_y, \omega_z)$ is a true absolute angular velocity in the projections to the RCS axes and $\hat{\omega}_{FOG} = (\omega_1, \omega_2, \omega_3)$ is the vector composed of the velocities measured by the first, second and third FOGs. Then the following can be written for each current time moment t:

$$\delta\hat{\omega}_{FOG}(t) = (E + \delta K) \cdot (F_H + \delta F) \cdot \bar{\omega}_{MGM}(t) + \delta\bar{\omega} + \bar{\xi}(t), \quad (1)$$

where E is the unitary matrix (3×3); $\delta K = \text{diag}(\delta k_1, \delta k_2, \delta k_3)$ is the diagonal matrix of relative errors of the FOG scale factors; F_H is known nominal matrix of the direction cosines (MDC) between the specified position of the FOG's SA and RCS axes (often it is a unitary matrix); δF is such matrix (3×3) of amendments to the nominal matrix of the direction cosines that:

$$\hat{F} \equiv F_H + \delta F = \{f_{ij}\}_{i,j=\overline{1,3}}$$

is the matrix of direction cosines as well but for the actual SA location; $\delta\bar{\omega}$ is the vector composed of the drifts of the first, second and third FOGs; $\bar{\xi}(t)$ is a three-dimensional vector of the noise component of measurements with a zero mean.

Relation (1) is a standard mathematical model of perturbed measurements made by the MGM in which parameters δK , δF , $\delta\bar{\omega}$, depending (in the general case) on the temperature factors correspond to the FOG instrumental errors. The reason for the introduced errors and the method of their recording in the perturbed measurement generally correspond to those which are standard in the optical gyroscopy and inertial navigation [15].

For the subsequent solution of the problem, there is no need to separate measurement scaling and transformation by means of MDC. Therefore, introduce notation:

$$F^* = (E + \delta K) \cdot (F_H + \delta F)$$

and rewrite (1) as:

$$\hat{\omega}_{FOG}(t) = F^* \cdot \bar{\omega}_{MGM}(t) + \delta\bar{\omega} + \bar{\xi}(t). \quad (2)$$

Application of the model in simulation modeling. The tasks of simulation modeling using formula (2) with a required time step are fulfilled by generation of the MGM measurements for an arbitrarily prescribed true rotational

speed $\bar{\omega}_{MGM}(t)$ and various temperature conditions of the instrument operation.

To do this, first the current model temperature values T_i^M at the points of location of the built-in temperature sensors are determined for each FOG by means of the finite-element calculation model of the non-stationary thermal field (Fig. 9). The matrix elements are then calculated:

$$F^* = \{f_{ij}^*\}_{i,j=\overline{1,3}},$$

using the following formula:

$$f_{ij}^*(\tau) = \phi_0^{(ij)} + \phi_1^{(ij)} \cdot \tau_i + \phi_2^{(ij)} \cdot \tau_i^2 + \phi_3^{(ij)} \cdot \tau_i^3, \quad i, j = \overline{1,3}, \quad (3)$$

and the drift values using the following formula:

$$\delta\omega_i(\tau_i) = k_{00}^{(i)} + k_{10}^{(i)} \cdot \tau_i + k_{20}^{(i)} \cdot \tau_i^2 + k_{30}^{(i)} \cdot \tau_i^3 + k_{01}^{(i)} \cdot \Delta\tau_i + k_{11}^{(i)} \cdot \tau_i \cdot \Delta\tau_i, \quad i = \overline{1,3}, \quad (4)$$

where

$$\tau_i = \frac{T_i^M - T_0}{\mathfrak{R}}$$

and

$$\Delta\tau_i = \frac{\Delta T_i^M}{\Delta T_{max}}$$

are normalized centered dimensionless values of temperature and the temperature gradient of the i-th FOG respectively;

$$T_0 = \frac{(T_{max} + T_{min})}{2}$$

is mean temperature of the working temperature range $[T_{min}, T_{max}]$;

$$\mathfrak{R} = \frac{T_{max} - T_{min}}{2}$$

is radius of the working temperature range; ΔT_i^M is the model value of the temperature gradient calculated as a time derivative from T_i^M ; ΔT_{max} is its maximum possible value;

$$\phi_0^{(ij)}, \phi_1^{(ij)}, \phi_2^{(ij)}, \phi_3^{(ij)}; k_{00}^{(i)}, k_{10}^{(i)}, k_{20}^{(i)}, k_{30}^{(i)}, k_{01}^{(i)}, k_{11}^{(i)}, \quad i, j = \overline{1,3}$$

are known parameters obtained at the pre-calibration stage for concrete FOG samples.

The structure and order of analytical models (3), (4) related to the instrumental errors were determined empirically in the preliminary studies [9]. It should be pointed out that for the specified FOG samples, truncated models in which there are no certain summands can be the most efficient by the results of calibration. In this case, without loss of generality, the corresponding coefficients can be assumed to be zero in models (3), (4).

During simulation of real FOG measurements, a problem of an adequate numerical simulation of the added noise is always taking place because the real noise component has a complex characteristic [16]. The problem disappears if the noise sample derived from the actual measurements of concrete FOG samples is used as a random component $\bar{\xi}(t)$. For this purpose, laboratory tests are carried out in stationary thermal conditions. Measurements are done and saved with a frequency equal to the simulation frequency. The sampling duration must not be less than the duration of the subsequent modeling.

Thus, after calibration of MGM using formula (2), the problem of data generation to simulate functioning of the gyroscopic system is solved.

MGM calibration. The algorithm for the model parameter calculation. The central moment of the above data generation procedure is obtaining coefficients of the temperature models (3), (4) which are used in it. To this end, so-called instrument calibration shall be done. Consider this problem in detail.

The problem under consideration is inverse to the problem of measurement generation and differs from the original one in that the gyroscope measurements are known and parameters of errors $\delta K, \delta F, \delta \bar{\omega}$ are the sought quantities. When doing this, the problem of calibration is solved based on the obtained experimental data and, as a rule, with the use of laboratory equipment and metrological support.

The calibration procedure includes the following:

- experimental data processing algorithm;
- requirements to the laboratory equipment and metrological support;
- schedule of carrying out calibration experiments;
- criteria for assessing the calibration efficiency;
- analysis of sources and the error level of the procedure implementation.

The model of MGM measurements is taken as the basis for derivation of calculation formulas of procedure (1). Assume that the calibration measurements are recorded at the time moments $t_n, n=1, 2, 3, \dots$ and performed at a constant rotational speed $\bar{\omega}_{MGM}$ and a constant FOG temperature. Since single FOG measurements have a significant noise, average them out by the formula:

$$\bar{\omega}_s = \frac{1}{N} \sum_{k=1}^N \hat{\omega}_{FOG}(t_{(s-1)N+k}), \quad (5)$$

where $\bar{\omega}_s$ is the calculated vector of the averaged measured angular velocity at the projections to the FOG's SA; $s=1, 2, 3, \dots$ is the number of the averaged value; N is the number of counts involved in the averaging.

In this case, expression (2) for the averaged values can be represented as:

$$F^* \cdot \bar{\omega}_{MGM}^{(s)} + \delta \bar{\omega} = \bar{\omega}_s, \quad (6)$$

where $\bar{\omega}_{MGM}^{(s)}$ is the known true angular velocity in the projections to the RCS axis at the s -th interval of averaging;

$$F^* = \{f_{ij}^*\}_{i,j=\overline{1,3}}, \quad \delta \bar{\omega} = \{\delta \omega_i\}_{i=\overline{1,3}}$$

are the sought parameters of the model.

The vector equation (6) disintegrates into three independent scalar equations:

$$\begin{pmatrix} 1 & \bar{\omega}_{MGM}^{(s)}[X] & \bar{\omega}_{MGM}^{(s)}[Y] & \bar{\omega}_{MGM}^{(s)}[Z] \end{pmatrix} \cdot \begin{pmatrix} f_{11}^* \\ f_{12}^* \\ f_{13}^* \end{pmatrix} = \bar{\omega}_s[i], \quad (7)$$

$i = \overline{1,3},$

where i is the gyroscope number;

$$\bar{\omega}_{MGM}^{(s)}[X], \bar{\omega}_{MGM}^{(s)}[Y], \bar{\omega}_{MGM}^{(s)}[Z]$$

are averaged projections of the absolute angular velocity of MGM rotation to axes X, Y, Z of RCS corresponding to the averaging interval with number s ; $\bar{\omega}_s[i]$ are averaged measurements of the i -th FOG.

Obviously, to calculate four parameters $\delta \omega_i, f_{11}^*, f_{12}^*, f_{13}^*$ one must have at least four equations of form (7) corresponding to various rotation modes. In this case, the determining system can be written for each $i = \overline{1,3}$ as ($s=1, 2, 3, 4$):

$$\begin{pmatrix} 1 & \bar{\omega}_{MGM}^{(1)}[X] & \bar{\omega}_{MGM}^{(1)}[Y] & \bar{\omega}_{MGM}^{(1)}[Z] \\ 1 & \bar{\omega}_{MGM}^{(2)}[X] & \bar{\omega}_{MGM}^{(2)}[Y] & \bar{\omega}_{MGM}^{(2)}[Z] \\ 1 & \bar{\omega}_{MGM}^{(3)}[X] & \bar{\omega}_{MGM}^{(3)}[Y] & \bar{\omega}_{MGM}^{(3)}[Z] \\ 1 & \bar{\omega}_{MGM}^{(4)}[X] & \bar{\omega}_{MGM}^{(4)}[Y] & \bar{\omega}_{MGM}^{(4)}[Z] \end{pmatrix} \cdot \begin{pmatrix} \delta \omega_i \\ f_{11}^* \\ f_{12}^* \\ f_{13}^* \end{pmatrix} = \begin{pmatrix} \bar{\omega}_1[i] \\ \bar{\omega}_2[i] \\ \bar{\omega}_3[i] \\ \bar{\omega}_4[i] \end{pmatrix}. \quad (8)$$

The sought model parameters are calculated from (8). For absence of degeneracy of system (8), specify the MGM rotation modes corresponding to different numbers s , in the form:

$$\bar{\omega}_{MGM}^{(1)} = (\omega, 0, 0), \quad \bar{\omega}_{MGM}^{(2)} = (0, \omega, 0),$$

$$\bar{\omega}_{MGM}^{(3)} = (0, 0, \omega), \quad \bar{\omega}_{MGM}^{(4)} = (m_1 \omega, m_2 \omega, m_3 \omega),$$

where ω, m_1, m_2, m_3 are parameters. For these conditions, the determinant of the system (8) matrix has the following form:

$$\Delta = (m_1 + m_2 + m_3 - 1) \cdot \omega^3,$$

which implies that for the solvability of (8) at $\omega \neq 0$ it is sufficient to specify:

$$m_1 + m_2 + m_3 \neq 1,$$

or, in particular, assume:

$$m_1 = 2, \quad m_2 = 0, \quad m_3 = 0,$$

which corresponds to the simplest mode of rotation.

Thus, to determine constant parameters:

$$F^* = \{f_{ij}^*\}_{i,j=\overline{1,3}} \quad \text{and} \quad \delta \bar{\omega} = \{\delta \omega_i\}_{i=\overline{1,3}}$$

it is enough to measure angular velocity in the four above-mentioned MGM rotation modes and solve the system (8) independently for each FOG using the averaged data.

The above-mentioned requirement of the FOG temperature constancy over four rotation modes can be excluded if $f_{ij}^*, \delta \omega_i$ parameters are sought in a form of (3), (4), i. e. in the following form:

$$\begin{pmatrix} \delta \omega_i \\ f_{11}^* \\ f_{12}^* \\ f_{13}^* \end{pmatrix} = H(\tau_i^{(s)}) \cdot \mu_i, \quad (9)$$

where

$$H(\tau_i^{(s)}) = H_i^{(s)} = \{h_{lm}\}_{l=\overline{1,4}, m=\overline{1,8}}$$

is the matrix consisting of zeros excepting the calculated elements:

$$\begin{aligned}
 h_{11} &= 1, h_{12} = \tau_i^{(s)}, h_{13} = (\tau_i^{(s)})^2, h_{14} = (\tau_i^{(s)})^3, \\
 h_{15} &= \Delta\tau_i^{(s)}, h_{16} = \tau_i^{(s)} \cdot \Delta\tau_i^{(s)}; \\
 h_{27} &= 1, h_{28} = \tau_i^{(s)}, h_{29} = (\tau_i^{(s)})^2, h_{2,10} = (\tau_i^{(s)})^3; \\
 h_{3,11} &= 1, h_{3,12} = \tau_i^{(s)}, h_{3,13} = (\tau_i^{(s)})^2, h_{3,14} = (\tau_i^{(s)})^3; \\
 h_{4,15} &= 1, h_{4,16} = \tau_i^{(s)}, h_{4,17} = (\tau_i^{(s)})^2, h_{4,18} = (\tau_i^{(s)})^3,
 \end{aligned}$$

$\tau_i^{(s)}$, $\Delta\tau_i^{(s)}$ are dimensionless temperature parameters of the i -th FOG in the averaging interval with number s ; μ_i is the column vector of the sought parameters of the temperature model:

$$\mu_i = \{k_{00}^{(i)}, k_{10}^{(i)}, k_{20}^{(i)}, k_{30}^{(i)}, k_{01}^{(i)}, k_{11}^{(i)}, \phi_0^{(i1)}, \phi_1^{(i1)}, \phi_2^{(i1)}, \phi_3^{(i1)}, \phi_0^{(i2)}, \phi_1^{(i2)}, \phi_2^{(i2)}, \phi_3^{(i2)}, \phi_0^{(i3)}, \phi_1^{(i3)}, \phi_2^{(i3)}, \phi_3^{(i3)}\}.$$

Substitute (9) in (7) to obtain the following scalar equation:

$$(w_{MGu}^{(s)})^T \cdot H_i^{(s)} \cdot \mu_i = \tilde{\omega}_s[i], \tag{10}$$

where

$$w_{MGu}^{(s)} = \{1, \tilde{\omega}_{MGu}^{(s)}[X], \tilde{\omega}_{MGu}^{(s)}[Y], \tilde{\omega}_{MGu}^{(s)}[Z]\}$$

is a column vector.

To find a 18-dimensional sought vector μ_i using equation (10), it is necessary to carry out at least 18 measuring sessions to get the system:

$$\begin{pmatrix} (w_{MGu}^{(1)})^T \cdot H_i^{(1)} \\ (w_{MGu}^{(2)})^T \cdot H_i^{(2)} \\ (w_{MGu}^{(3)})^T \cdot H_i^{(3)} \\ (w_{MGu}^{(4)})^T \cdot H_i^{(4)} \\ \dots \\ (w_{MGu}^{(L)})^T \cdot H_i^{(L)} \end{pmatrix} \cdot \mu_i = \begin{pmatrix} \tilde{\omega}_1[i] \\ \tilde{\omega}_2[i] \\ \tilde{\omega}_3[i] \\ \tilde{\omega}_4[i] \\ \dots \\ \tilde{\omega}_L[i] \end{pmatrix}, \tag{11}$$

where $L \geq 18$.

For solvability of such system, it is sufficient to repeat several times the above four MGM rotation modes at different FOG temperatures. The system redundancy (concerning the number of equations) which appears in this case is exhausted when using the least squares method whereby the following is obtained:

$$\mu_i = (\Pi_i^T \cdot \Pi_i)^{-1} \Pi_i^T \cdot \tilde{W}_i, \tag{12}$$

where Π_i is designation for the block matrix in the left part of (11); \tilde{W}_i is designation of the vector in the right parts.

Thus, determination of parameters of the FOG temperature model of measurements includes:

- procedure of averaging measurements by formula (5);
- composition of a redundant system of linear equations (11);
- decision (12) by the method of least squares.

Hardware requirements and the experiment schedule. Describe conditions and procedure of the calibration experiment.

To carry out the calibration experiments, it is necessary to use a two- or three-axis motion simulator like those produced by Actdyn Systemes (France) [17]. The simulator must be mounted in a horizontal plane with an accuracy not worse

than 5'' and ensure MGM rotation at a predetermined angular velocity. The studied MGM is placed in the heating and cooling chamber (HCC) of Acutronic type and attached to the simulator for a conjoint motion. To account for the Earth's rotational speed, terrestrial latitude must be known with accuracy better than 10'' for the location where the experiment is conducted. In the course of the experiment, the gyro output data and the measurements of the embedded temperature sensors are recorded with a required update rate.

The approximate order of the experiment is as follows:

0. Cool the switched off MGM down to the T_{min} temperature.
1. Enable HCC by the programs executed sequentially and coordinated with the operational modes of the FOG being the part of the gyroscopic system:
 - external temperature varying from T_{min} to T_{max} with a positive gradient T_{max} ;
 - external temperature varying from T_{max} to T_{min} with a negative gradient ΔT_{max} .
2. Enable MGM and data logging.
3. Direct the RCS X axis vertically upwards. Spin at a rate of +20°/s around the vertical axis for 10 minutes.
4. Direct the RCS Y axis vertically upwards. Spin at a rate of +20°/s around the vertical axis for 10 minutes.
5. Direct the RCS Z axis vertically upwards. Spin at a rate of +20°/s around the vertical axis for 10 minutes.
6. Direct the RCS X axis vertically upwards. Spin at a rate of +40°/s around the vertical axis for 10 minutes.
7. Repeat items 3-6 to the end of work by the HCC program.
8. Complete data logging and process the results.

Remarks:

- a) rotation speed and duration of the modes are given approximately. In practice, they should be adjusted taking into account the specific type of FOG;
- b) items 3–6 correspond to the previously introduced four rotation modes;
- c) when processing, data corresponding to the transition from one mode to another rotation mode are ignored.

The described schedule enables an adequate assessment of parameters of the temperature model of the FOG measurements by the method of least squares.

Criteria of calibration efficiency.

Qualitative assessment of the experimental-data approximation using statistical mean value and statistical mean square deviation (MDS) of the approximation error calculated for the sample being used is well known [18]. In the problem under consideration, such assessment should be appropriately used to select the best structure of the approximating models, but objectively it does not reflect the calibration efficiency.

Efficiency of MGM calibration depends on the parametric stability of temperature dependencies of the instrumental errors caused by the instrument itself. In these conditions, it is proposed to use the magnitude of the dispersion range of the FOG IE of the same name as a criterion of effectiveness. These errors are identified based on the results of several independent experiments under equivalent conditions.

This implies that for an objective appraisal of the calibration efficiency, it is necessary to conduct a series of similar calibration experiments and statistically process their results.

The assessments of the relative error of the scale factors collected in a matrix are the most obvious results of calibration:

$$\delta K = \text{diag}(\delta k_1, \delta k_2, \delta k_3),$$

assessments of the FOG SA misalignment amendments:

$$\delta F = \left\{ \delta f_{ij} \right\}_{i,j=1,3},$$

and zero drift assessment. However, within the frames of the developed procedure, the following elements alongside the $\delta \bar{\omega}$ are directly computed: f_{ij}^* , $i, j = 1, 3$.

Matrices F^* are associated with abovementioned parameters by following relations:

$$f_{ij}^* = (1 + \delta k_i) \cdot (f_{ij}^H + \delta f_{ij}),$$

in which f_{ij}^H are elements of the known nominal matrix of direction cosines. Hence, it is easy to obtain the following for the sought assessments by positioning f_{ij}^* :

$$\begin{aligned} \delta k_i &= \sqrt{(f_{i1}^*)^2 + (f_{i2}^*)^2 + (f_{i3}^*)^2} - 1, \\ \delta f_{ij} &= \frac{f_{ij}^*}{(1 + \delta k_i)} - f_{ij}^H, \quad i, j = \overline{1, 3}. \end{aligned} \quad (13)$$

At the same time, it is easy to assess non-orthogonality of the i th FOG's sensitivity axis relative to the RCS based on δf_{ij} elements.

Assuming that the implemented IE values are "exactly" determined for each calibration experiment corresponding to one switching of the instrument, calibration efficiency is characterized by the magnitude of the similar-error scatter interval. Concrete results of the study are as follows.

Six equivalent calibration experiments have been conducted in stationary temperature conditions for the MGM incorporating three FOGs of a medium accuracy class having "almost orthogonal" sensitivity axes. With the use of the above-described procedure, FOG's instrumental errors were calculated and mean values and MSD of the same-name errors were defined for the entire series (Table 1).

The mean error values show that the studied FOGs really correspond to the medium-class accuracy. At the same time, a high level of the estimate repeatability (as it is evidenced by the fairly small values of MSD) means that a significant (several times) improvement of the FOG accuracy for all parameters can be achieved using algorithmic compensation taking into account mean values of the error estimates. In addition, the obtained statistical characteristics permit adequate simulation of the MGM functioning for various kinds of switching.

Hence, the experimental results have shown consistency of the introduced criterion of calibration efficiency.

Sources of the procedure errors and recommendations for practical application.

The main source of the method errors in the developed calibration procedure is incorrect account for the Earth's rotation during result processing. This factor can be eliminated by using (in the calculation formulas) the measurement values averaged within the time interval during which IGM makes a complete revolution around the rotary axis of the stand. In this case, the effect of the horizontal component of the Earth angular velocity on the FOG readings will be automatically compensated with a high accuracy. The vertical component of the Earth angular velocity should be taken into account in the projection to the vertical axis of the RCS vector of the true rotation velocity.

Table 1

Results of calibration experiments

FOG number	Zero drift, °/hr		Correction to the scale factor, %		Maximal parameter of nonorthogonality, '	
	mean value	MSD	mean value	MSD	mean value	MSD
FOG No. 1	0.18	0.02	-0.16	0.001	14.27	0.02
FOG No. 2	-0.36	0.04	-0.24	0.001	16.47	0.63
FOG No. 3	-0.02	0.02	0.34	0.002	25.32	0.03

The procedure effectiveness can also be affected by instrumental factors:

- nonhorizontality of the stand;
- conical motion of the stand axis of rotation;
- uneven rotation;
- rough repeatability of angular positions of the stand, etc.

Some of these factors can be eliminated by an additional calibration of the module using algorithms of inertial calculation that goes beyond the scope of this article.

Basic recommendations for the practical application of the procedure can be stated without validation as follows:

- FOG measurement averaging should be carried out in a time interval during which the MGM makes one or more complete turns around the stand axis;
- the procedure can be applied to an arbitrary number of FOGs with axes of sensitivity randomly positioned relative to the RCS;
- the approximation problem can be solved using a redundant data set. Under these conditions, it is advisable to use a recursive least-squares method with a rising volume of measurements for assessment of the sought model parameters;
- the measurement error estimates obtained during calibration can be used not only for simulation modeling of the MGM operation but also to compensate for the measurement errors in the course of the block operation. The corresponding model of restoration of the angular rotation velocity in the projections to the RCS axis has the following form:

$$\bar{\omega}_{MGM}(t_n) = (F^M)^{-1} \cdot (\hat{\omega}_{FOG}(t_n) - \delta \bar{\omega}^M), \quad (14)$$

where $\delta \bar{\omega}^M$, F^M are the model values of the drift vector and the transformation matrix the elements of which are calculated according to the formulas (3), (4) with an account for current values of the FOG temperature and its gradient.

7. Discussion of the results obtained in the study of the temperature models of the FOG measurement errors

The advantage of this approach is integration of the procedure for calculating the heat field in the instrument and the task of construction and use of the temperature dependent models of the FOG instrumental errors. This approach increases efficiency of the simulation modeling of various gyroscopic systems in the arbitrarily specified temperature conditions. In particular, the procedure for calculating heat fields provides an estimate of temperature at any time moment and anywhere in the instrument including the point of location of the built-in temperature sensor. In view of this assessment and the measurement error models, FOG measurements

are generated with their accuracy characteristics being close to real ones. These measurements are proposed to be further used in the application software (AS) of the gyroscopic system directly for the solution of functional tasks facing it. Thus, the developed approach ensures more precise consideration for the temperature dependence of the MGM measurement errors and an eventual improvement of efficiency and simulation veracity in designing gyroscopic systems.

However, the role of the proposed method is not limited thereto. In the future, it can also be used, firstly, to refine composition and location of temperature sensors in the MGM in order to improve quality of the measurement error compensation in the subsequent operation of the instrument and secondly, to improve the layout of the electronic and structural components of the MGM in terms of reducing influence of the perturbing thermal factors.

8. Conclusions

1. New experimental data of the temporal variation of temperature at various points of the fiber optic gyroscope and the heat camera were obtained.

2. Based on the finite element method, a computational model of the thermal field in the FOG at various outside temperatures was developed. Comparison of experimental data with the results of finite element calculation of non-stationary heat conduction problems has demonstrated their quite

satisfactory agreement. The verification studies enabled the use of the developed calculation model for further analysis of the instrument thermal conditions. The calculation model is further used in solving the problem of simulation modeling of the FOG measurements as a part of MGM.

3. Temperature models of the FOG instrumental errors were considered. With their help, the MGM output data for all kinds of thermal conditions are predicted with an accuracy close to real sensor errors. For the adequacy of these models, their parameters are pre-defined in the course of calibration of concrete FOG samples. A procedure for calibration of the models of IGM errors was developed. It is remarkable for the possibility of joint identification of all IEs using a single redundant volume of measurements.

4. To assess the effectiveness of FOG calibration methods, it was proposed to use the magnitude of the repeatability interval of the same-name errors. Such an interval can be obtained by carrying out several independent calibration experiments under equivalent conditions. Experimentally determined estimates of effectiveness of such calibration demonstrate its practical value.

Thus, the results obtained in the present study are first of all aimed at improvement of accuracy of the gyroscopic systems based on the mid-end FOGs used in aerospace engineering and secondly, they make the basis for further studies of thermal processes taking place in FOGs and optimization of the MGM design as a whole.

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Проведена порівняльна характеристика багатокритеріальних задач оптимізації, критерії яких можуть мати кількісну і якісну природу. Обґрунтовано рішення щодо вибору зразка безпілотного літального апарату для прийняття на озброєння за характеристиками, значення яких прогножуються в умовах нестохастичної невизначеності на основі експертних даних. Запропонована декомпозиція проблеми в ієрархію, що відображає зміст багатокритеріальної задачі оптимізації

Ключові слова: безпілотний літальний апарат, декомпозиція проблеми в ієрархію, лінгвістична змінна

Проведена сравнительная характеристика многокритериальных задач оптимизации, критерии которых могут быть количественной и качественной природы. Обоснованно решение относительно выбора образца беспилотного летательного аппарата для принятия на вооружение с характеристиками, значения которых прогнозируются в условиях нестохастической неопределенности на основе экспертных данных. Предложена декомпозиция проблемы в иерархию, которая отражает содержание многокритериальной задачи оптимизации

Ключевые слова: беспилотный летательный аппарат, декомпозиция проблемы в иерархию, лингвистическая переменная

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SELECTING A MODEL OF UNMANNED AERIAL VEHICLE TO ACCEPT IT FOR MILITARY PURPOSES WITH REGARD TO EXPERT DATA

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1. Introduction

Defensive military doctrine of the Armed Forces of Ukraine (AFU) establishes high requirements for all elements of combat readiness and for training troops. The Armed Forces must be prepared to fight off aggression by

conducting defensive actions. The most important task of the headquarters under defensive nature of the military doctrine is permanent surveillance of the enemy that should provide for a timely and organized transition of troops from peace to war. The main role in this is assigned to the intelligence. A number of tasks for aerial reconnaissance can be solved