

**ABSTRACT AND REFERENCES**  
**APPLIED MECHANICS**

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**AN INCREASE OF THE LOADING CAPACITY  
AND RELIABILITY OF GEARS BY METHODS  
OF OPTIMIZING INVOLUTE GEARING  
PARAMETERS (p. 6–15)**

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A large volume of rocks containing valuable minerals is treated at mining and processing plants in Kazakhstan. Ball mills and rod mills are used for their grinding and further processing.

Ball mills with gear drive rings in the drums suffer from intense wear of the teeth due to the heavy mode of the mill operation. It thus necessitates their frequent replacement and long mill downtime. The gears of the ball mill drive experience an intense impact stress, which reduces the resource of their operation and the mill as a whole due to wear.

The article presents research on developing rational parameters of involute gearing, aimed at increasing the loading capacity of the gear as well as reducing the overall dimensions, noise, and vibration. In order to solve the set tasks, dynamic processes are simulated, modification of the teeth is proposed, and the task of designing the initial meshing contour is solved when the line of the tooth profile is slightly deviated from the involute curve of the tooth surface.

The kinematic and dynamic parameters of a tooth transmission influencing the wear resistance of teeth are found out, and also the influence of the loading capacity under conditions of stable lubrication is determined.

Because of the complexity of modifying a large diameter of the driven gear wheel, it is proposed to modify only the teeth of the driving wheel, both at their tops and legs.

**Keywords:** ball mill, tooth wear, involute gearing, tooth modification, tooth profile line.

**References**

- Bolotovskiy, I. A. (1997). Spravochnik po geometricheskому расчету эволвентных зубчатых и червячных передач. Moscow: Mashinostroenie, 448.
- Vulgakov, E. B., Dorofeev, B. L. (2002). Komp'yuternoe проектирование эволвентных зубчатых передач в обобщенных параметрах. Конверсиya v mashinostroenii, 6, 148–151.
- Kapelevich, A. L., Shekhtman, Y. V. (2009). Tooth Fillet Profile Optimization for Gears with Symmetric and Asymmetric Teeth. Gear Technology, 73–79.
- Kapelevich, A. L., Shekhtman, Y. V. (2016). Rating of asymmetric tooth gears. Power transmissing, 40–45.
- Zorko, D., Tavčar, J., Duhovnik, J. (2018). The influence of the tooth profile shape on the stress-strain state in the gear. International Scientific Journal «Machines. Technologies. Materials.», 12 (4), 153–156.
- Jelaska, D. (2012). Gears and Gear Drives. John Wiley & Sons. doi: <https://doi.org/10.1002/9781118392393>
- Križan, B. (1995). Numerical procedure for obtaining the gears' addendum modification coefficients based on the sliding friction loss minimum. In International Congress «Gear Transmissions».
- Klein, B. (1988). Übertragungseigenschaften von Verzahnungsgeometrien. Technica, 37 (5), 15–24.
- Povetkin, V. V., Kerimzhanova, M. F., Isaeva, I. N., Orlova, E. P. (2016). Качество изготавления тяжелонагруженных зубчатых передач и его влияние на износостойкость'. Promышленност' Kazakhstan, 6 (99), 52–54.
- Tayts, B. A., Markov, N. N. (1978). Tochnost' i kontrol' Zubchatyh peredach. Leningrad: Mashinostroenie, 136.
- Timofeev, B. P., Abramchuk, M. V. (2010). Normy tochnosti Zubchatyh koles i peredach: nuzhen noviy standart. Standarty i kachestvo, 5, 60–63.
- Dorofeev, V. L., Golovanov, V. V., Dorofeev, D. V. (2013). Sistema modelirovaniya «AEROFLANK» & prymoy sintez iznosostoykih i maloshumnyh Zubchatyh peredach. Visnyk NTU «KhPI». Serya: Problemy mehanichnogo pryvodu, 40 (1013), 40–49.
- Tiwari, S. K., Joshi, U. K. (2012). Stress Analysis of mating involute spur gear teeth. International Journal of Engineering Research and Technology, 1 (9).
- Unkov, E. P., Dzhonson, U., Kolmogorov, V. L. et. al.; Unkov, E. P., Ovchinnikov, A. G. (Ed.) (1983). Teoriya plasticheskikh deformatsiy metallov. Moscow: Mashinostroenie, 598.
- Shi, J., Gou, X., Zhu, L. (2019). Modeling and analysis of a spur gear pair considering multi-state mesh with time-varying parameters and backlash. Mechanism and Machine Theory, 134, 582–603. doi: <https://doi.org/10.1016/j.mechmachtheory.2019.01.018>
- Huang, K., Xiong, Y., Wang, T., Chen, Q. (2017). Research on the dynamic response of high-contact-ratio spur gears influenced by surface roughness under EHL condition. Applied Surface Science, 392, 8–18. doi: <https://doi.org/10.1016/j.apsusc.2016.09.009>
- Karpat, F., Yuce, C., Doğan, O. (2020). Experimental measurement and numerical validation of single tooth stiffness for involute spur gears. Measurement, 150, 107043. doi: <https://doi.org/10.1016/j.measurement.2019.107043>
- Thirumurugan, R., Gnanasekar, N. (2019). Investigation of the effect of load distribution along the face width and load sharing between the pairs in contact on the fracture parameters of the spur gear tooth with root crack. Engineering Failure Analysis, 97, 518–533. doi: <https://doi.org/10.1016/j.engfailanal.2019.01.051>
- Artoni, A. (2019). A methodology for simulation-based, multiobjective gear design optimization. Mechanism and Machine Theory, 133, 95–111. doi: <https://doi.org/10.1016/j.mechmachtheory.2018.11.013>
- Sánchez, M. B., Pleguezuelos, M., Pedrero, J. I. (2019). Influence of profile modifications on meshing stiffness, load sharing, and transmission error of involute spur gears. Mechanism and Machine Theory, 139, 506–525. doi: <https://doi.org/10.1016/j.mechmachtheory.2019.05.014>
- Luo, Y., Baddour, N., Liang, M. (2019). Dynamical modeling and experimental validation for tooth pitting and spalling in spur

- gears. Mechanical Systems and Signal Processing, 119, 155–181. doi: <https://doi.org/10.1016/j.ymssp.2018.09.027>
22. Dorofeev, V., Dorofeev, D., Zhuravlev, V., Edinovich, A. (2015). The use of the software complex AEROFLANK for calculating the load distribution across the width of the teeth, the deflection of the shafts and of the forces acting on the supports. Progressivnye tehnologii i sistemy mashinostroeniya, 1 (51), 56–62.
  23. Timofeev, B. P., Abramchuk, M. V. (2007). Sravnenie tablichnykh znacheniy parametrov tochnosti zubchatyh koles i peredach v standartah: ISO 1328 i GOST 1643-81. Zubchatye peredachi. Available at: <http://tmm.spbstu.ru/9/timofeev-9.pdf>

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## A SEMI-ANALYTICAL METHOD FOR ANALYS OF CONTACT INTERACTION BETWEEN STRUCTURAL ELEMENTS ALONG ALIGNED SURFACES (p. 16–25)

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A significant share of structures includes the components that are in contact with each other. These include, for example, stamps, molds, machine tools, technological equipment, engines, etc. They are characterized by a varied load mode. Therefore, an important aspect in studying the stressed-strained state of such structures is to determine the dependence of contact pressure on the external forces applied to them. A superposition principle for contact problems is not applicable in a general case. However, for this type of structures, the linear dependence of contact pressure on the load level has been established. In this case, the contact area does not depend on the load level. It has been demonstrated that this pattern holds not only for a one-component but also for the multi-component load. As a result, the possibility for rapid determining the stressed-strained state of such structures is ensured, while maintaining the accuracy of the results obtained.

The applicability of the constructed method has been demonstrated by using the machine tools' clamping accessories as an example. The established patterns are important when estimating the designs of structures. The derived direct proportional dependence of the solution on the applied loads makes it possible to shorten the design time of structures with the elements that interact when they are in contact at surfaces of the matching shape. In this case, we have considered different sets of loads, as well as the various varying variants of these loads. The examined cases have confirmed the direct proportionality of the components of the stressed-strained state of the magnitude of the applied forces for the case of their coordinated

change. It has been also shown under an uneven change in the individual components of loads the dependence of contact pressure and components of the stressed-strained state of the examined objects on the applied forces demonstrates a complex character different from the directly proportional relation. The established dependences underlie the substantiation of the design and technological parameters of the structures that are designed, as well as their operational modes.

**Keywords:** contact pressure, stressed-strained state, theory of variational inequalities, machine tool, region of contact interaction

## References

1. Johnson, K. L. (1985). Contact Mechanics. Cambridge University Press. doi: <https://doi.org/10.1017/cbo9781139171731>
2. Rogovyi, A. (2018). Energy performances of the vortex chamber supercharger. Energy, 163, 52–60. doi: <https://doi.org/10.1016/j.energy.2018.08.075>
3. Rogovyi, A., Khovanskyy, S. (2017). Application of the similarity theory for vortex chamber superchargers. IOP Conference Series: Materials Science and Engineering, 233, 012011. doi: <https://doi.org/10.1088/1757-899x/233/1/012011>
4. Rogovyi, A., Khovanskyy, S., Grechka, I., Pitel, J. (2019). The Wall Erosion in a Vortex Chamber Supercharger Due to Pumping Abrasive Mediums. Advances in Design, Simulation and Manufacturing II, 682–691. doi: [https://doi.org/10.1007/978-3-030-22365-6\\_68](https://doi.org/10.1007/978-3-030-22365-6_68)
5. Gaydamaka, A., Kulik, G., Frantsuzov, V., Hrechka, I., Khovanskyi, S., Rogovyi, A. et. al. (2019). Devising an engineering procedure for calculating the ductility of a roller bearing under a no-central radial load. Eastern-European Journal of Enterprise Technologies, 3 (7 (99)), 6–10. doi: <https://doi.org/10.15587/1729-4061.2019.168145>
6. Syomin, D., Rogovyi, A. (2012). Features of a Working Process and Characteristics of Irrotational Centrifugal Pumps. Procedia Engineering, 39, 231–237. doi: <https://doi.org/10.1016/j.proeng.2012.07.029>
7. Panchenko, A., Voloshina, A., Boltynsky, O., Milaeva, I., Grechka, I., Khovanskyy, S. et. al. (2018). Designing the flow-through parts of distribution systems for the PRG series planetary hydraulic motors. Eastern-European Journal of Enterprise Technologies, 3 (1 (93)), 67–77. doi: <https://doi.org/10.15587/1729-4061.2018.132504>
8. Panchenko, A., Voloshina, A., Kiurchev, S., Titova, O., Onopreychuk, D., Stefanov, V. et. al. (2018). Development of the universal model of mechatronic system with a hydraulic drive. Eastern-European Journal of Enterprise Technologies, 4 (7 (94)), 51–60. doi: <https://doi.org/10.15587/1729-4061.2018.139577>
9. Panchenko, A., Voloshina, A., Milaeva, I., Panchenko, I., Titova, O. (2018). The Influence of the form Error after Rotor Manufacturing on the Output Characteristics of an Orbital Hydraulic Motor. International Journal of Engineering & Technology, 7 (4.3), 1. doi: <https://doi.org/10.14419/ijet.v7i4.3.19542>
10. Voloshina, A., Panchenko, A., Boltynskiy, O., Panchenko, I., Titova, O. (2018). Justification of the Kinematic Diagrams for the Distribution System of a Planetary Hydraulic Motor. International Journal of Engineering & Technology, 7 (4.3), 6. doi: <https://doi.org/10.14419/ijet.v7i4.3.19544>
11. Voloshina, A., Panchenko, A., Boltynsky, O., Titova, O. (2019). Improvement of Manufacture Workability for Distribution Systems of Planetary Hydraulic Machines. Advances in Design, Simulation and Manufacturing II, 732–741. doi: [https://doi.org/10.1007/978-3-030-22365-6\\_73](https://doi.org/10.1007/978-3-030-22365-6_73)
12. Martynyak, R. M., Slobodyan, B. S. (2009). Contact of elastic half spaces in the presence of an elliptic gap filled with liquid. Materials Science, 45 (1), 66–71. doi: <https://doi.org/10.1007/s11003-009-9156-9>
13. Slobodyan, B. S., Lyashenko, B. A., Malanchuk, N. I., Marchuk, V. E., Martynyak, R. M. (2016). Modeling of Contact Interaction of Periodically Textured Bodies with Regard for Frictional Slip. Journal

- of Mathematical Sciences, 215 (1), 110–120. doi: <https://doi.org/10.1007/s10958-016-2826-x>
14. Kravchuk, A. S., Neittaanmäki, P. J. (2007). Variational and Quasi-Variational Inequalities in Mechanics. Springer. doi: <https://doi.org/10.1007/978-1-4020-6377-0>
  15. Vollebregt, E., Segal, G. (2014). Solving conformal wheel–rail rolling contact problems. Vehicle System Dynamics, 52 (sup1), 455–468. doi: <https://doi.org/10.1080/00423114.2014.906634>
  16. Kalker, J. J. (1977). Variational Principles of Contact Elastostatics. IMA Journal of Applied Mathematics, 20 (2), 199–219. doi: <https://doi.org/10.1093/imamat/20.2.199>
  17. Papangelo, A., Hoffmann, N., Ciavarella, M. (2017). Load-separation curves for the contact of self-affine rough surfaces. Scientific Reports, 7 (1). doi: <https://doi.org/10.1038/s41598-017-07234-4>
  18. Ciavarella, M. (2015). Adhesive rough contacts near complete contact. International Journal of Mechanical Sciences, 104, 104–111. doi: <https://doi.org/10.1016/j.ijmecsci.2015.10.005>
  19. Ciavarella, M., Joe, J., Papangelo, A., Barber, J. R. (2019). The role of adhesion in contact mechanics. Journal of The Royal Society Interface, 16 (151), 20180738. doi: <https://doi.org/10.1098/rsif.2018.0738>
  20. Li, Q., Popov, V. L. (2018). Adhesive force of flat indenters with brush-structure. Facta Universitatis, Series: Mechanical Engineering, 16 (1), 1. doi: <https://doi.org/10.22190/fume1712200051>
  21. Li, S., Yao, Q., Li, Q., Feng, X.-Q., Gao, H. (2018). Contact stiffness of regularly patterned multi-asperity interfaces. Journal of the Mechanics and Physics of Solids, 111, 277–289. doi: <https://doi.org/10.1016/j.jmps.2017.10.019>
  22. Popov, V. L., Pohrt, R., Li, Q. (2017). Strength of adhesive contacts: Influence of contact geometry and material gradients. Friction, 5 (3), 308–325. doi: <https://doi.org/10.1007/s40544-017-0177-3>
  23. Ciavarella, M. (2017). A very simple estimate of adhesion of hard solids with rough surfaces based on a bearing area model. Meccanica, 53 (1-2), 241–250. doi: <https://doi.org/10.1007/s11012-017-0701-6>
  24. Ciavarella, M. (2017). On Pastewka and Robbins' Criterion for Macrosopic Adhesion of Rough Surfaces. Journal of Tribology, 139 (3). doi: <https://doi.org/10.1115/1.4034530>
  25. Argatov, I., Li, Q., Pohrt, R., Popov, V. L. (2016). Johnson-Kendall-Roberts adhesive contact for a toroidal indenter. Proceedings of the Royal Society A: Mathematical, Physical and Engineering Sciences, 472 (2191), 20160218. doi: <https://doi.org/10.1098/rspa.2016.0218>
  26. Ciavarella, M. (2018). An approximate JKR solution for a general contact, including rough contacts. Journal of the Mechanics and Physics of Solids, 114, 209–218. doi: <https://doi.org/10.1016/j.jmps.2018.03.005>
  27. Li, Q., Pohrt, R., Lyashenko, I. A., Popov, V. L. (2019). Boundary element method for nonadhesive and adhesive contacts of a coated elastic half-space. Proceedings of the Institution of Mechanical Engineers, Part J: Journal of Engineering Tribology, 234 (1), 73–83. doi: <https://doi.org/10.1177/1350650119854250>
  28. Li, Q., Popov, V. L. (2017). Boundary element method for normal non-adhesive and adhesive contacts of power-law graded elastic materials. Computational Mechanics, 61 (3), 319–329. doi: <https://doi.org/10.1007/s00466-017-1461-9>
  29. Rey, V., Anciaux, G., Molinari, J.-F. (2017). Normal adhesive contact on rough surfaces: efficient algorithm for FFT-based BEM resolution. Computational Mechanics, 60 (1), 69–81. doi: <https://doi.org/10.1007/s00466-017-1392-5>
  30. Atroshenko, O., Tkachuk, M. A., Martynenko, O., Tkachuk, M. M., Saverska, M., Hrechka, I., Khovanskyi, S. (2019). The study of multi-component loading effect on thinwalled structures with bolted connections. Eastern-European Journal of Enterprise Technologies, 1 (7 (97)), 15–25. doi: <https://doi.org/10.15587/1729-4061.2019.154378>
  31. Atroshenko, O., Bondarenko, O., Ustinenko, O., Tkachuk, M., Diomina, N. (2016). A numerical analysis of non-linear contact tasks for the system of plates with a bolted connection and a clearance in the fixture. Eastern-European Journal of Enterprise Technologies, 1 (7 (79)), 24. doi: <https://doi.org/10.15587/1729-4061.2016.60087>
  32. Tkachuk, M. M., Skripchenko, N. B., Tkachuk, M. A. (2016). Solving of problems on contact interaction of rough bodies using model of nonlinear Winkler layer. Mekhanika ta mashynobuduvannia, 1, 3–14.
  33. Tkachuk, M. (2018). A numerical method for axisymmetric adhesive contact based on Kalker's variational principle. Eastern-European Journal of Enterprise Technologies, 3 (7 (93)), 34–41. doi: <https://doi.org/10.15587/1729-4061.2018.132076>
  34. Tkachuk, M. M., Skripchenko, N., Tkachuk, M. A., Grabovskiy, A. (2018). Numerical methods for contact analysis of complex-shaped bodies with account for non-linear interface layers. Eastern-European Journal of Enterprise Technologies, 5 (7 (95)), 22–31. doi: <https://doi.org/10.15587/1729-4061.2018.143193>
  35. Tkachuk, M., Bondarenko, M., Grabovskiy, A., Sheychenko, R., Grabovskiy, R., Posohov, V. et al. (2018). Thinwalled structures: analysis of the stressed-strained state and parameter validation. Eastern-European Journal of Enterprise Technologies, 1 (7 (91)), 18–29. doi: <https://doi.org/10.15587/1729-4061.2018.120547>
  36. Tkachuk, N. A., Kravchenko, S. A., Pylev, V. A., Parsadanov, I. V., Grabovsky, A. V., Veretennik, O. V. (2019). Discrete and Continual Strengthening of Contacting Structural Elements: Conception, Mathematical and Numerical Modeling. Science & Technique, 18 (3), 240–247. doi: <https://doi.org/10.21122/2227-1031-2019-18-3-240-347>
  37. Bondarenko, M., Tkachuk, M., Grabovskiy, A., Hrechka, I. (2019). Substantiation of Thin-Walled Structures Parameters Using Non-linear Models and Method of Response Surface Analysis. International Journal of Engineering Research in Africa, 44, 32–43. doi: <https://doi.org/10.4028/www.scientific.net/jera.44.32>
  38. Washizu, K. (1982). Variational Methods in Elasticity & Plasticity. Oxford-New York: Pergamon Press, 630.
  39. Zienkiewicz, O. C., Taylor, R. L., Zhu, J. Z. (2013). The Finite Element Method: Its Basis and Fundamentals. Butterworth-Heinemann, 756. doi: <https://doi.org/10.1016/c2009-0-24909-9>
  40. Karmanov, V. G. (2004). Matematicheskoe programmirovaniye. Moscow: FIZMATLIT, 264.
  41. Tkachuk, M. M., Grabovskiy, A., Tkachuk, M. M., Hrechka, I., Ishchenko, O., Domina, N. (2019). Investigation of multiple contact interaction of elements of shearing dies. Eastern-European Journal of Enterprise Technologies, 4 (7 (100)), 6–15. doi: <https://doi.org/10.15587/1729-4061.2019.174086>
  42. Tkachuk, M., Grabovskiy, A., Tkachuk, M. M., Zarubina, A., Saverska, M., Mukhin, D., Kutsenko, S. (2019). Contact interaction of molds elements and project-technological provision of their technical. Bulletin of the National Technical University «KhPI» Series: Engineering and CAD, 1, 58–66. doi: <https://doi.org/10.20998/2079-0775.2019.1.07>
  43. Sea, Zh. (1973). Optimizatsiya. Teoriya i algoritmy. Moscow: Mir, 244.
  44. Himmelblau, D. M. (1975). Prikladnoe nelineynoe programmirovaniye. Moscow, 534.

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**CONSTRUCTION OF AN ALGORITHM TO  
ANALYTICALLY SOLVE A PROBLEM ON THE  
FREE VIBRATIONS OF A COMPOSITE PLATE OF  
VARIABLE THICKNESS (p. 26–33)**

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The paper reports an algorithm to analytically solve one of the problems in the mechanics of elastic bodies, which is associated with studying the natural vibrations of a composite two-stage plate whose concave part is smoothly aligned with the part of a constant thickness. We have defined patterns for stating the boundary and transitional conditions, which should be taken into account when considering the natural vibrations of a two-stage plate.

The ratios have been obtained, which make it possible to study the distribution of deflections and determine the values of amplitudes of the curved vibrations of the plate. It was noted that the modes of vibrations are based on the symmetry and factorization methods that we had developed and refined earlier. Specifically, it has been found that the deflections can be explored through expressions that are derived through the sum of relevant solutions to two linear second-order differential equations with variable coefficients.

Based on the proposed approach, a system consisting of eight homogeneous algebraic equations has been defined, which allowed us to build a frequency equation for the plate rigidly fixed along the inner contour and free along the outer contour. We have determined the values for the plate's natural frequencies for the first three modes of natural vibrations. Moreover, in order to verify and expand a set of plates of different configurations, the plates with two types of concave in their variable part have been considered. The new approaches and the ratios based on them could be useful for the further advancement of methods for solving similar problems in mathematical physics on natural values. A practical implementation is the problems about the vibrations of plates with variable thickness and of different modes.

**Keywords:** natural frequencies, vibration modes, analytical solution, annular plate, free vibrations, symmetry method.

## References

1. Panovko, Ya. G. (1967). Osnovy prikladnoy teorii uprugih kolebaniy. Moscow: Mashinostroenie, 316.
2. Bitseno, K. B., Grammel', R. (1952). Tehnicheskaya dinamika. Vol. II. Moscow: GITTL, 638.
3. Hrinchenko, V. T., Didkovskyi, V. S., Matsypura, V. T. (1998). Teoriychni osnovy akustyky. Kyiv: IZMN, 376.
4. Naida, S., Didkovskyi, V., Pavlenko, O., Naida, N. (2019). Objective Audiometry Based on the Formula of the Middle Ear Parameter: A New Technique for Researches and Differential Diagnosis of Hearing. 2019 IEEE 39th International Conference on Electronics and Nanotechnology (ELNANO). doi: <https://doi.org/10.1109/elnano.2019.8783502>
5. Kvashnin, S. E. (1990). Proektirovaniye ul'trazvukovykh stomatologicheskikh volnovodov-instrumentov. Ul'trazvuk v stomatologii. Kuybyshev, 32–36.
6. Kovalenko, A. D. (1959). Kruglye plastinki peremennoy tolshchiny. Moscow: Fizmatgiz, 294.
7. Zhou, D., Lo, S. H. (2011). Three-dimensional vibrations of annular thick plates with linearly varying thickness. Archive of Applied Mechanics, 82 (1), 111–135. doi: <https://doi.org/10.1007/s00419-011-0543-y>
8. Semnani, S. J., Attarnejad, R., Firouzjaei, R. K. (2013). Free vibration analysis of variable thickness thin plates by two-dimensional differential transform method. Acta Mechanica, 224 (8), 1643–1658. doi: <https://doi.org/10.1007/s00707-013-0833-2>
9. Yalcin, H. S., Arikoglu, A., Ozkol, I. (2009). Free vibration analysis of circular plates by differential transformation method. Applied Mathematics and Computation, 212 (2), 377–386. doi: <https://doi.org/10.1016/j.amc.2009.02.032>
10. Kornilov, A. A. (1968). Kolebaniya kol'tsevoy plastiny peremennoy tolshchiny proizvol'nogo profilya s uchetom inertsii vrashcheniya i deformatsii sviga. Vestnik KPI. Seriya: Mashinostroenie, 8, 62–68.
11. Hasheminejad, S. M., Ghaheri, A. (2013). Exact solution for free vibration analysis of an eccentric elliptical plate. Archive of Applied Mechanics, 84 (4), 543–552. doi: <https://doi.org/10.1007/s00419-013-0816-8>
12. Viswanathan, K. K., Javed, S., Aziz, Z. A., Prabakar, K. (2015). Free vibration of symmetric angle-ply laminated annular circular plate of variable thickness under shear deformation theory. Meccanica, 50 (12), 3013–3027. doi: <https://doi.org/10.1007/s11012-015-0175-3>
13. Powmya, A., Narasimhan, M. C. (2015). Free vibration analysis of axisymmetric laminated composite circular and annular plates using Chebyshev collocation. International Journal of Advanced Structural Engineering, 7 (2), 129–141. doi: <https://doi.org/10.1007/s40091-015-0087-4>
14. Sabir, K. (2018). A variant of the polygonal plate oscillation problem solution. Journal of Mechanical Science and Technology, 32 (4), 1563–1567. doi: <https://doi.org/10.1007/s12206-018-0310-x>
15. Chen, L., Cheng, Y. M. (2017). The complex variable reproducing kernel particle method for bending problems of thin plates on elastic foundations. Computational Mechanics, 62 (1), 67–80. doi: <https://doi.org/10.1007/s00466-017-1484-2>
16. Panda, S., Barik, M. (2017). Large amplitude free flexural vibration of arbitrary thin plates using superparametric element. International Journal of Dynamics and Control, 5 (4), 982–998. doi: <https://doi.org/10.1007/s40435-016-0275-5>
17. Salawu, S. A., Sobamowo, G. M., Sadiq, O. M. (2019). Investigation of dynamic behaviour of circular plates resting on Winkler and Pasternak foundations. SN Applied Sciences, 1 (12). doi: <https://doi.org/10.1007/s42452-019-1588-8>
18. Burmeister, D. (2017). Asymmetric buckling of shell-stiffened annular plates. International Journal of Mechanics and Materials in Design, 14 (4), 565–575. doi: <https://doi.org/10.1007/s10999-017-9390-5>
19. Trapezon, K. O. (2014). The decision of task about the axisymmetric natural vibrations of circular plate with a thickness decreasing from a center on a concave parabola. Electronics and Communications, 19 (5), 98–106. doi: <https://doi.org/10.20535/2312-1807.2014.19.5.38881>
20. Abramowitz, M., Stegun, I. (Eds.) (1972). Handbook of mathematical functions with formulas, graphs, and mathematical tables. Applied mathematics series 55, USA.
21. Trapezon, K. A. (2012). Method of symmetries at the vibrations of circular plates of variable thickness. Elektronika i svyaz', 6, 66–77.

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**THE STRESSED-DEFORMED STATE OF SLAB REINFORCED-CONCRETE HOLLOW STRUCTURES CONSIDERING THE BIAXIAL COMPRESSION OF CONCRETE (p. 34–42)**

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In order to significantly reduce the weight of flat monolithic reinforced concrete floors, foundations, and other slab structures, construction operations have increasingly involved effective inserts as the separate articles made from relatively light and cheap materials that are placed in the midsection and left in the slabs after concreting.

The inserts made from relatively light and cheap materials, with respect to concrete, have the strength and rigidity that are orders of magnitude less and are essentially used to form hollows. The inserts considered in this paper are prismatic. When the inserts are arranged in two directions, which is typical for most slab structures, we obtain the I-sections, whose calculation involved the analysis of the impact exerted by the general and local strength factors. Under such conditions, slabs must be calculated taking into consideration the biaxial work of concrete. In this paper, we have examined the stressed-strained state of the slab reinforced concrete structures with a bidirectional location of inserts and have substantiated the estimation schemes and calculation dependences related to the procedure for calculating the floors and other slab reinforced concrete structures with a bidirectional location of inserts. The paper gives an example of the calculation of a monolithic flooring slab based on the proposed procedure, which demonstrated that accounting for the biaxial stressed-strained state of concrete significantly increases the strength of concrete and the rigidity of a flooring slab, by 19.3 %.

Thus, the consideration of biaxial compression of concrete is an important factor in the design of slab structures with a bidirectional arrangement of inserts.

**Keywords:** reinforced concrete hollow structures, stressed-strained state, biaxial compression of concrete, estimation schemes, strength, rigidity, example of calculation.

## References

- Melnyk, I. V., Sorokhtei, V. M., Prystavskyi, T. V. (2018). Ploski zalizobetonni plytni konstruktsii z efektyvnymy vstavkamy. Lviv, 272.
- Tsvetkov, K. A., Mitrokhina, A. O. (2013). Features of the effect of dynamic loading produced on the concrete behavior at different stages of deformation caused by uniaxial and biaxial compression. Vestnik MGSU, 7, 77–85. doi: <https://doi.org/10.22227/1997-0935.2013.7.77-85>
- Gang, H., Kwak, H.-G. (2017). A strain rate dependent orthotropic concrete material model. International Journal of Impact Engineering, 103, 211–224. doi: <https://doi.org/10.1016/j.ijimpeng.2017.01.027>
- Quast, M., Curbach, M. (2017). Concrete under biaxial dynamic compressive loading. Procedia Engineering, 210, 24–31. doi: <https://doi.org/10.1016/j.proeng.2017.11.044>
- Quast, M., Curbach, M. (2015). Behaviour of concrete under biaxial dynamic loading. Proceeding of Fifth International Workshop on Performance, Protection and Strengthening of Structures under Extreme Loading – PROTECT, 3–10. Available at: [https://books.google.com.ua/books?id=9c4OCgAAQBAJ&pg=PA10&lpg=PA10&dq=M.+Curbach,+M.+Quast,+Concrete+under+biaxial+impact+loading,+in:+S.+Hiermaier+\(ed.\)&source=bl&ots=e-R5fj6aOH&sig=ACfU3U170x4D0YgUj13CF3tRP3yadvuI](https://books.google.com.ua/books?id=9c4OCgAAQBAJ&pg=PA10&lpg=PA10&dq=M.+Curbach,+M.+Quast,+Concrete+under+biaxial+impact+loading,+in:+S.+Hiermaier+(ed.)&source=bl&ots=e-R5fj6aOH&sig=ACfU3U170x4D0YgUj13CF3tRP3yadvuI)
- A&hl=ru&sa=X&ved=2ahUKewi8itTu8NLLAhVrwosKHZ\_\_B7cQ6AEwAnoECAkQAQ#v=onepage&q=M.%20Curbach%2C%20M.%20Quast%2C%20Concrete%20under%20biaxial%20impact%20loading%2C%20in%3A%20S.%20Hiermaier%20(ed.)&f=true
- Deng, Z., Sheng, J., Wang, Y. (2018). Strength and Constitutive Model of Recycled Concrete under Biaxial Compression. KSCE Journal of Civil Engineering, 23 (2), 699–710. doi: <https://doi.org/10.1007/s12205-018-0575-8>
- Ivashenko, Y., Ferder, A. (2019). Experimental studies on the impacts of strain and loading modes on the formation of concrete «stress-strain» relations. Construction and Building Materials, 209, 234–239. doi: <https://doi.org/10.1016/j.conbuildmat.2019.03.008>
- Charpin, L., Le Pape, Y., Coustabeau, É., Toppani, É., Heinfling, G., Le Bellego, C. et al. (2018). A 12 year EDF study of concrete creep under uniaxial and biaxial loading. Cement and Concrete Research, 103, 140–159. doi: <https://doi.org/10.1016/j.cemconres.2017.10.009>
- Hampel, T., Speck, K., Scheerer, S., Ritter, R., Curbach, M. (2009). High-Performance Concrete under Biaxial and Triaxial Loads. Journal of Engineering Mechanics, 135 (11), 1274–1280. doi: [https://doi.org/10.1061/\(ASCE\)0733-9399\(2009\)135:11\(1274\)](https://doi.org/10.1061/(ASCE)0733-9399(2009)135:11(1274))
- Rong, C., Shi, Q., Zhang, T., Zhao, H. (2018). New failure criterion models for concrete under multiaxial stress in compression. Construction and Building Materials, 161, 432–441. doi: <https://doi.org/10.1016/j.conbuildmat.2017.11.106>
- Bambura, A. N., Davidenko, A. I. (1989). Eksperimental'nye issledovaniya zakonomernosti deformirovaniya betona pri dvuhosnom szhatii. Stroitel'nye konstruktsii, 42, 95–100.
- Mel'nyk, I. V. (2015). Analysis of the Stiffnesses of Reinforced-Concrete Plane Monolithic Floors with Tubular Inserts. Materials Science, 50 (4), 564–570. doi: <https://doi.org/10.1007/s11003-015-9754-7>
- Kupfer, H., Gerstle, K. (1973). Behavior of concrete under biaxial stresses. Journal of the Engineering Mechanics Division, 99 (4), 853–866.
- Gvozdev, A. A., Yashin, A. V., Petrova, K. V. et al. (1978). Neodnoosnye napryazhenno-deformirovannye sostoyaniya betona. Prochnost', strukturnye izmeneniya i deformatsii betona. Moscow: Stroyizdat, 196–222.
- Bambura, A. M., Dorogova, O. V., Sazonova, I. R. (2017). Preliminary determination of the tensile reinforcement area for structures with rectangular section if bending. Nauka ta budivnytstvo, 3, 32–39.
- Babaiev, V. M., Bambura, A. M., Pustovoitova, O. M. et al. (2015). Praktychnyi rozrakhunok elementiv zalizobetonnykh konstruktsiy za DBN V.2.6-98:2009 v porivnianni z rozrakhunkamy za SNyP 2.03.01-84\* i EN 1992-1-1 (Eurocode 2). Kharkiv: Zoloti storinky, 240.

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**DETERMINATION OF THE WORKFLOW  
OF ENERGY-SAVING VIBRATION UNIT  
WITH POLYPHASE SPECTRUM OF  
VIBRATIONS (p. 43–49)**

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A new scheme for the excitation of vibrations of the working bodies of the blocks of a vibration unit based on a change in the phase angles of unbalances between themselves is developed. The implementation of such an idea allows for one revolution of imbalances to realize the number of vibration actions on the technological environment, how many vibration units the installation has. Thus, the frequency spectrum is implemented, which significantly increases the efficiency of the process. The proposed scheme is suitable for the implementation of various processes with a reduction in energy consumption compared to existing designs of vibration machines. A design diagram of a vibration unit with four vibration blocks is developed. A mathematical model is selected based on the representation of machine parameters as discrete, and the processing medium as continuous. The simulation of the working process of the vibration unit is based on the use of the finite element method. The finite element model is composed by approximating all the supporting elements, including the shaping surfaces, by two-dimensional finite elements.

Vibration isolating supports and elastic elements of the model are adopted three-dimensional, since the processes occurring in such structural elements are more complex in terms of energy dissipation. The workflow of an energy-saving vibration unit that implements polyphase vibrations is investigated. The equations of motion of such a system are compiled and the amplitudes and frequencies of vibrations that determine this movement are determined. The distribution of the amplitudes of the vibrations along the perimeter of the frame, mounted on the vibration blocks of the vibration unit, is estimated. The possibility of efficient use of the polyphase spectrum of vibrations when performing the processes of sorting and compaction of materials based on the implementation of shear and normal stresses is determined. The proposed scheme of an energy-saving vibration unit and certain parameters open up a real opportunity for creating a new class of machines for use in various industries. The obtained results are used in the design of an energy-saving design of a vibration unit with a rational choice of phase angles for compaction of process media.

**Keywords:** vibration unit, vibration blocks, unbalance, model, phase angles, amplitudes, frequencies and vibration modes.

**References**

1. Nesterenko, M. P. (2015). Progressive development of vibration equipment with spatial oscillations for forming concrete products. *Zbirnyk naukovykh prats. Seriya: Haluzeve mashynobuduvannia, budivnytstvo*, 2, 16–23.
2. Maslov, O., Salenko, Yu., Maslova, N. (2011). Doslidzhennia vzaemodiyi vibruiuchoi plyty z tsementobetonnoiu sumishshiu. *Visnyk KNU imeni Mykhaila Ostrohradskoho*, 2, 93–98.
3. Mishchuk, E. O. (2014). Theoretical research of working process of the vibration jaw crusher. *Zbirnyk naukovykh prats. Seriya: haluzeve mashynobuduvannia, budivnytstv*, 3 (42), 70–77.
4. Gursky, V., Kuzio, I., Lanets, O., Kisala, P., Tolegenova, A., Syzdykpayeva, A. (2019). Implementation of dual-frequency resonant vibratory machines with pulsed electromagnetic drive. *Przeglad elektrotechniczny*. doi: <https://doi.org/10.15199/48.2019.04.08>
5. Lanets, O., Derevenko, I., Borovets, V., Kovtunyuk, M., Komada, P., Mussabekov, K., Yeraliyeva, B. (2019). Substantiation of consolidated inertial parameters of vibrating bunker feeder. *Przeglad elektrotechniczny*. doi: <https://doi.org/10.15199/48.2019.04.09>
6. Andò, B., Baglio, S., Bulsara, A. R., Marletta, V., Pistorio, A. (2015). Experimental and Theoretical Investigation of a Nonlinear Vibrational Energy Harvester. *Procedia Engineering*, 120, 1024–1027. doi: <https://doi.org/10.1016/j.proeng.2015.08.701>
7. Yamamoto, G. K., da Costa, C., da Silva Sousa, J. S. (2016). A smart experimental setup for vibration measurement and imbalance fault detection in rotating machinery. *Case Studies in Mechanical Systems and Signal Processing*, 4, 8–18. doi: <https://doi.org/10.1016/j.csmspp.2016.07.001>
8. Jia, Y., Seshia, A. A. (2014). An auto-parametrically excited vibration energy harvester. *Sensors and Actuators A: Physical*, 220, 69–75. doi: <https://doi.org/10.1016/j.sna.2014.09.012>
9. Cacciola, P., Banjanac, N., Tombari, A. (2017). Vibration Control of an existing building through the Vibrating Barrier. *Procedia Engineering*, 199, 1598–1603. doi: <https://doi.org/10.1016/j.proeng.2017.09.065>
10. Yin, Y., Su, Y., Wang, Z. (2017). Vibration characteristics of casting string under the exciting force of an electric vibrator. *Natural Gas Industry B*, 4 (6), 457–462. doi: <https://doi.org/10.1016/j.ngib.2017.09.007>
11. Chmelnizkij, A., Nagula, S., Grabe, J. (2017). Numerical Simulation of Deep Vibration Compaction in Abaqus/CEL and MPM. *Procedia Engineering*, 175, 302–309. doi: <https://doi.org/10.1016/j.proeng.2017.01.031>
12. Mahadevaswamy, P., Suresh, B. S. (2016). Optimal mass ratio of vibratory flap for vibration control of clamped rectangular plate. *Ain Shams Engineering Journal*, 7 (1), 335–345. doi: <https://doi.org/10.1016/j.asej.2015.11.014>
13. Michalczyc, J. (2012). Inaccuracy in self-synchronisation of vibrators of two-drive vibratory machines caused by insufficient stiffness of vibrators mounting. *Archives of Metallurgy and Materials*, 57 (3), 823–828. doi: <https://doi.org/10.2478/v10172-012-0090-8>
14. Bernyk, I., Luhovskyi, O., Nazarenko, I. (2018). Effect of rheological properties of materials on their treatment with ultrasonic cavitation. *Materiali i Tehnologije*, 52 (4), 465–468. doi: <https://doi.org/10.17222/mit.2017.021>
15. Nazarenko, I. I., Pentyuk, B. N., Chovnyuk, Y. V. (2006). Vibration-wave stress concentrators removing flashes in molding and pressing powder materials. *Refractories and Industrial Ceramics*, 47 (5), 294–298. doi: <https://doi.org/10.1007/s11148-006-0112-z>
16. Babić, M., Čali, M., Nazarenko, I., Fragassa, C., Ekinovic, S., Mihaliková, M. et. al. (2018). Surface roughness evaluation in hardened materials by pattern recognition using network theory. *International Journal on Interactive Design and Manufacturing (IJIDeM)*, 13 (1), 211–219. doi: <https://doi.org/10.1007/s12008-018-0507-3>
17. Nazarenko, I. I., Ruchynskyi, M. M., Sviderskyi, A. T., Kobylanska, I. M., Kalizhanova, A., Kozbakova, A. (2019). Development of energy-efficient vibration machines for the building-and-construction industry. *Przeglad Elektrotechniczny*. doi: <https://doi.org/10.15199/48.2019.04.10>
18. Nazarenko, I., Sviderskyi, A., Diedov, O. (2011). Stvorennia vysokoeffektivnykh vibroushchilniuichykh mashyn novoho pokolinnia.

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**ESTABLISHING CONDITIONS FOR THE OCCURRENCE OF DYNAMIC AUTO-BALANCING IN A ROTOR ON TWO ELASTIC-VISCOUS SUPPORTS (p. 50–57)**

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Were found the conditions for occurrence of dynamic auto-balancing for the case of a rotor mounted on two elastic-viscous supports, balanced by two or more passive auto-balancers of any type.

A modernized energy method has been applied under assumption that the mass of auto-balancers' loads is much smaller than the rotor mass. The method has been constructed for rotors on isotropic elastic-viscous supports, when such bodies are attached to the rotor, whose relative motion is hindered by elastic and viscous resistance forces. The method makes it possible to find stationary motions of the rotary system, assess their stability. At stationary motions the relative motions of the attached bodies stop, and the system rotates as a whole around the axis of rotation formed by the supports.

The mechanical and mathematical model of the system has been described. We have found the generalized potential under stationary motions, as well as a dissipative function corresponding to the supports. For the generalized rotor coordinates the equations of stationary motions of the system have been derived. The reduced potential has been investigated for a conditional extremum under an assumption that the equations of stationary

motions hold, which correspond to the generalized coordinates of the rotor.

It has been established that dynamic balancing of the rotor is possible only for the case of a long rotor, two or more auto-balancers of any type, installed in different correction planes and only at the rotor rotation speeds exceeding resonance ones. It has been found that the resistance forces in the supports do not change the conditions for auto-balancing occurrence explicitly, but they can change these conditions implicitly – by changing the region of existence of stationary motions.

The result obtained coincides with the result that was derived from using a generalized empirical criterion for auto-balancing occurrence when damping in the supports is not taken into consideration. It has been shown that the modernized energy method (as well as the generalized empirical criterion for auto-balancing occurrence) makes it possible to find generalized conditions for auto-balancing occurrence, suitable for any type of auto-balancers. Therefore, both methods are applicable for building a general theory of passive auto-balancers, suitable for auto-balancers of any type.

**Keywords:** rotor, isotropic support, auto-balancer, stationary motion, motion stability, equation of steady motion.

**References**

1. Thearle, E. L. (1950). Automatic dynamic balancers (Part 2 – Ring, pendulum, ball balancers). Machine Design, 22 (10), 103–106.
2. Gusalov, A. A. (2002). Avtobalansiruyushchie ustroystva pryamogo deystviya. Moscow: Nauka, 119.
3. Filimonikhin, H. B. (2004). Zrinvazhennia i vibrozakhyst rotoriv avtobalansyramy z tverdymy koryhuvalnymy vantazhamy. Kirovograd: KNTU, 352.
4. Nesterenko, V. P. (1985). Avtomaticheskaya balansirovka rotirov priborov i mashin so mnogimi stepenyami svobody. Tomsk: Izd-vo Tomsk. un-ta, 84.
5. Sperling, L., Ryzhik, B., Duckstein, H. (2001). Two-plain automatic balancing. Machine Dynamics Problems, 25 (3/4), 139–152.
6. Rodrigues, D. J., Champneys, A. R., Friswell, M. I., Wilson, R. E. (2008). Automatic two-plane balancing for rigid rotors. International Journal of Non-Linear Mechanics, 43 (6), 527–541. doi: <https://doi.org/10.1016/j.ijnonlinmec.2008.01.002>
7. Bolton, J. N. (2010). Single- and Dual-Plane Automatic Balancing of an Elastically-Mounted Cylindrical Rotor with Considerations of Coulomb Friction and Gravity. Blacksburg, Virginia, 338.
8. Rodrigues, D. J., Champneys, A. R., Friswell, M. I., Wilson, R. E. (2011). Two-plane automatic balancing: A symmetry breaking analysis. International Journal of Non-Linear Mechanics, 46 (9), 1139–1154. doi: <https://doi.org/10.1016/j.ijnonlinmec.2011.04.033>
9. Lu, C.-J., Wang, M.-C. (2011). Stability analysis of a ball-rod-spring automatic balancer. International Journal of Mechanical Sciences, 53 (10), 846–854. doi: <https://doi.org/10.1016/j.ijmecsci.2011.07.005>
10. Rezaee, M., Mohammad Ettefagh, M., Fathi, R. (2019). Dynamics and Stability of Non-Planar Rigid Rotor Equipped with Two Ball-Spring Autobalancers. International Journal of Structural Stability and Dynamics, 19 (02), 1950001. doi: <https://doi.org/10.1142/s0219455419500019>
11. Gorbenko, A. N., Shmelev, S. Kh. (2018). Necessary Self-Balancing Robustness Conditions for a Two-Bearing Rotor Taking Unbalance Mass into Account. Herald of the Bauman Moscow State Technical University. Series Mechanical Engineering, 5, 36–50. doi: <https://doi.org/10.18698/0236-3941-2018-5-36-50>
12. Filimonikhin, G., Filimonikhina, I., Dumenko, K., Lichuk, M. (2016). Empirical criterion for the occurrence of auto-balancing and its application for axisymmetric rotor with a fixed point and isotropic elastic support. Eastern-European Journal of Enterprise Technologies, 5 (7 (83)), 11–18. doi: <https://doi.org/10.15587/1729-4061.2016.79970>

13. Filimonikhin, G., Filimonikhina, I., Yakymenko, M., Yakimenko, S. (2017). Application of the empirical criterion for the occurrence of auto-balancing for axisymmetric rotor on two isotropic elastic supports. Eastern-European Journal of Enterprise Technologies, 2 (7 (86)), 51–58. doi: <https://doi.org/10.15587/1729-4061.2017.96622>
14. Filimonikhin, G., Filimonikhina, I., Ienina, I., Rahulin, S. (2019). A procedure of studying stationary motions of a rotor with attached bodies (auto-balancer) using a flat model as an example. Eastern-European Journal of Enterprise Technologies, 3 (7 (99)), 43–52. doi: <https://doi.org/10.15587/1729-4061.2019.169181>
15. Muyzhniek, A. I. (1959). Nekotorye voprosy teorii avtomaticheskoy dinamicheskoy balansirovki. Voprosy dinamiki i prochnosti, 6, 123–145.
16. Strauch, D. (2009). Classical Mechanics: An Introduction. Springer-Verlag Berlin Heidelberg, 405. doi: <https://doi.org/10.1007/978-3-540-73616-5>
17. Ruelle, D. (1989). Elements of Differentiable Dynamics and Bifurcation Theory. Academic Press, 196. doi: <https://doi.org/10.1016/c2013-0-11426-2>

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## DEVELOPMENT OF DYNAMIC INTEGRAL EVALUATION METHOD OF TECHNICAL STATE OF ONE-SECTION ELECTRIC LOCOMOTIVE BODY (p. 57–64)

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At present, one of the main problems arising from the long-term operation of one-section electric locomotives is the need to maintain their good technical condition. In this case, the determining aspect is often rapid identification of existing defects and damage to the main bearing structural elements of machine bodies, as well as preventing their development into more serious structural deviations.

The aim of the study is to develop a specialized method that allows identifying defects of the main bearing structural elements of the bodies of one-section electric locomotives at the early stages of emergence and development. This method of dynamic integral evaluation is based on the analysis of partial dynamic spectrum of the electric locomotive. Based on the magnitude of the spectrum deviation relative to the theoretical one obtained from finite element modeling, it is possible to determine the approximate nature and location of damage, especially latent.

The frequency spectrum of the main bearing structural elements of the bodies of one-section electric locomotives obtained in the course of the studies is rather dense and lies in the frequency range up to 20 Hz. The presence of damage reduces its value, and for the most common types of defects, this reduction is 25–30 %.

The effectiveness of the practical application of the dynamic integral evaluation method is illustrated by the example of the DS3-008 machine. The method revealed hidden damage to one of the elements of the bearing frame of the front surface of the cab, which was not revealed during the standard maintenance procedure of the machine. The use of the method of dynamic integral evaluation of the technical condition of electric locomotives is quite versatile and can also be recommended for other units of railway rolling stock.

In practice, the introduction of this approach will effectively prevent the development of emergencies.

**Keywords:** one-section electric locomotive, maintenance, dynamic integral evaluation method, technical condition.

## References

1. Loza, P. A., Grishechkina, T. S. (2015). Estimation of the quality of implementation electric rolling stock maintenance system. Elektryfikatsiya transportu, 9, 87–93.
2. Bannikov, D., Radkevich, A. (2019). Analytical method for compiling and applying a ballast map for the traction unit PE2U. Eastern-European Journal of Enterprise Technologies, 2 (1 (98)), 6–14. doi: <https://doi.org/10.15587/1729-4061.2019.160423>
3. Gureva, A., Chernetska-Biletska, N. (2015). Fundamentals of modeling of processes of maintenance of locomotives. Visnyk Skhidnoukrainskoho natsionalnogo universytetu imeni Volodymyra Dalia, 1 (218), 262–265.
4. Bodnar, B. E., Ochkasov, O. B., Bodnar, E. B., Hryshechkina, T. S., Ocheretnyuk, M. V. (2018). Simulation of locomotive repair organization by the methods of queue systems theory. Science and Transport Progress. Bulletin of Dnipropetrovsk National University of Railway Transport, 5 (77), 28–40. doi: <https://doi.org/10.15802/stp2018/147740>
5. Myamlin, S., Kalivoda, J., Neduzha, L. (2017). Testing of Railway Vehicles Using Roller Rigs. Procedia Engineering, 187, 688–695. doi: <https://doi.org/10.1016/j.proeng.2017.04.439>
6. Skrebkov, A. V., Vorobiyov, A. A., Lamkyn, A. G., Bodrikov, D. I. (2017). The study of running and maintenance process of electric locomotives with big data and simulation modeling tools. Byulleten' rezul'tatov nauchnyh issledovanij, 4, 190–198.
7. Bodnar, B., Ochkasov, O. (2017). System Choice of the Technical Maintenance of Locomotives Equipped with on-Board Diagnostic Systems. Transport Means: Proc. of 21st Intern. Sci. Conf. Pt. I. Juodkrante, 43–47.
8. Wang, G., Zeng, G., Cui, X., Feng, S. (2019). Dispersion analysis of the gradient weighted finite element method for acoustic problems in one, two, and three dimensions. International Journal for Numerical Methods in Engineering, 120 (4), 473–497. doi: <https://doi.org/10.1002/nme.6144>
9. Bean, M., Yi, S.-Y. (2019). A monolithic mixed finite element method for a fluid-structure interaction problem. Applied Mathematics and Computation, 363, 124615. doi: <https://doi.org/10.1016/j.amc.2019.124615>
10. Chimakurthi, S. K., Reuss, S., Tooley, M., Scampoli, S. (2017). ANSYS Workbench System Coupling: a state-of-the-art computational framework for analyzing multiphysics problems. Engineering with Computers, 34 (2), 385–411. doi: <https://doi.org/10.1007/s00366-017-0548-4>
11. Sapietová, A., Novák, P., Sága, M., Šulka, P., Sapieta, M. (2019). Dynamic and Stress Analysis of a Locking Mechanism in the Ansys Workbench Software Environment. Advances in Science and Technology Research Journal, 13 (1), 23–28. doi: <https://doi.org/10.12913/22998624/101601>
12. Chaomei, C., Chengjie, X., Haichuan, T., Guo, M. (2015). A Topology Optimization Method based on Nastran Card Quickly Modifying Parameter. Journal of Mechanical Transmission, 39 (7), 182–186.
13. Salahuddin, M. B. M., Atikah, A. F., Rosnah, S., Zuhair, M. N. M. (2019). Conceptual design and finite element analysis of a high inclusion dough shaping machine using 3D-computer aided design (CAD) (SolidWorks). Materialwissenschaft Und Werkstofftechnik, 50 (3), 267–273. doi: <https://doi.org/10.1002/mawe.201800205>
14. Liang, W., Rui-lin, L., Chang-hao, W. (2015). Modal Analysis and Improvement of Vibration Noise of Paper Folding Board Based on COSMOSWorks. Packaging Engineering, 1, 125–128.

15. Fialko, S., Karpilovskyi, V. (2018). Time history analysis formulation in SCAD FEA software. *Journal of Measurements in Engineering*, 6 (4), 173–180. doi: <https://doi.org/10.21595/jme.2018.20408>
16. Bannikov, D. O. (2018). Usage of construction-oriented software scad for analysis of work of machine-building structures. *Science and Transport Progress. Bulletin of Dniproprostrovsk National University of Railway Transport*, 1 (73), 98–111. doi: <https://doi.org/10.15802/stp2018/123406>
17. Blohin, E. P., Kostritsa, S. A., Chumak, V. V., Ostroverhov, N. P., Sultan, A. V., Datsenko, V. N., Krivchikov, A. E. (2004). Rezul'taty prochnostnyh ispytaniy elektrovozoa DS3. *Visnyk Dnipropetrovskoho natsionalnoho universytetu zaliznychnoho transportu imeni akademika V. Lazariana*, 5, 13–16.
18. Blohin, E. P., Pshin'ko, A. N., Korostenko, M. L., Granovskiy, R. B., Garkavi, N. Ya., Dzichkovskiy, E. M. (2004). Dinamika skorostnogo elektrovozoa tipa DS3. *Visnyk Dnipropetrovskoho natsionalnoho universytetu zaliznychnoho transportu imeni akademika V. Lazariana*, 5, 9–12.

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## SUBSTANTIATING THE OPTIMIZATION OF THE LOAD-BEARING STRUCTURE OF A HOPPER CAR FOR TRANSPORTING PELLETS AND HOT AGGLOMERATE (p. 65–74)

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The strength parameters have been determined for the bearing structure of a hopper car used to transport pellets and hot agglomerate. The calculation was based on a finite element method, implemented in the software COSMOSWorks. Strength reserves of load-bearing elements in a carbody have been determined. In order to reduce material consumption for a carbody, it has been proposed to use pipes with a circular cross-section as the bearing elements. Mathematical modeling was applied to determine the accelerations that act on the optimized bearing structure of a wagon when it is struck at shunting. It has been established that the accelerations that act on the bearing structure of a wagon amount to  $42.4 \text{ m/s}^2$  (4.3 g). The derived acceleration magnitude was accounted for when calculating the strength of a hopper car's bearing structure. The maximum equivalent stresses in this case reached about 270 MPa and were concentrated in the region where a girder beam interacts with a pivot beam while not exceeding the permissible ones for the grade of steel used in the metallic structure.

We have simulated the vertical dynamics of the optimized bearing structure of a hopper car used to transport pellets and hot agglomerate. During calculations, the parameters for a spring suspension of the 18-100 model's undercarriage were taken into consid-

eration. The results of our calculations make it possible to conclude that the accelerations of a hopper car body, as well as undercarriages, are within the allowable limits. In this case, in terms of compliance with the requirements of normative documents, the car ride quality can be described as «excellent».

The proposed technical solutions justify the use of round pipes as the load-bearing elements of a hopper car body for transporting pellets and hot agglomerate. In this case, it becomes possible to reduce the hopper car tare by almost 5 % compared to a prototype car. In addition, the introduction of round pipes in the bearing structure of a hopper car could bring down manufacturing costs for railroad car building enterprises.

Our study would contribute to the construction of modern structures of hopper cars, as well as to the improved efficiency of railroad transportation.

**Keywords:** hopper car, specialized freight car, bearing structure, car body strength, dynamic loading, car body optimization.

## References

1. Lukin, V. V., Shadur, L. A., Koturanov, V. I., Hohlov, A. A., Anisimov, P. S. (2000). *Konstruirovaniye i raschet vagonov*. Moscow, 731.
2. Vatulia, G., Falendysh, A., Orel, Y., Pavliuchenkov, M. (2017). Structural Improvements in a Tank Wagon with Modern Software Packages. *Procedia Engineering*, 187, 301–307. doi: <https://doi.org/10.1016/j.proeng.2017.04.379>
3. Kebal, Y., Shatov, V., Tokotyev, A., Murashova, N. (2017). Improving the design of hopper wagons for transporting grain. *Zbirnyk naukovykh prats DETUT. Seriya: «Transportni sistemy i tekhnolohiyi»*, 30, 113–122.
4. Serpik, I. N., Sudarev, V. G., Tyutyunnikov, A. I., Levkovich, F. N. (2008). Evolyutsionnoe modelirovanie v proektirovaniy nesushchih sistem vagonov. *Vestnik Vserossiyskogo Nauchno-Issledovatel'skogo Instituta Zhelezodorozhnoho Transporta*, 5, 21–25.
5. Beyn, D. G. (2011). Analiz napryazhennogo sostoyaniya nesushchego nastila pola chetyrekhosnogo poluvagona s gluhim kuzovom. *Vestnik Bryanskogo gosudarstvennogo tehnicheskogo universiteta*, 1 (29), 47–51.
6. Kuczek, T., Szachniewicz, B. (2015). Topology optimisation of railcar composite structure. *International Journal of Heavy Vehicle Systems*, 22 (4), 375. doi: <https://doi.org/10.1504/ijhvs.2015.073206>
7. Lee, H.-A., Jung, S.-B., Jang, H.-H., Shin, D.-H., Lee, J. U., Kim, K. W., Park, G.-J. (2015). Structural-optimization-based design process for the body of a railway vehicle made from extruded aluminum panels. *Proceedings of the Institution of Mechanical Engineers, Part F: Journal of Rail and Rapid Transit*, 230 (4), 1283–1296. doi: <https://doi.org/10.1177/0954409715593971>
8. Mrzygłód, M., Kuczek, T. (2013). Uniform crashworthiness optimization of car body for high-speed trains. *Structural and Multidisciplinary Optimization*, 49 (2), 327–336. doi: <https://doi.org/10.1007/s00158-013-0972-z>
9. Kučera, P., Pištěk, V. (2017). Testing of the mechatronic robotic system of the differential lock control on a truck. *International Journal of Advanced Robotic Systems*, 14 (5), 172988141773689. doi: <https://doi.org/10.1177/1729881417736897>
10. Pistek, V., Klimes, L., Mauder, T., Kucera, P. (2017). Optimal design of structure in rheological models: an automotive application to dampers with high viscosity silicone fluids. *Journal of Vibroengineering*, 19 (6), 4459–4470. doi: <https://doi.org/10.21595/jve.2017.18348>
11. Alyamovskiy, A. A. (2007). *SolidWorks/COSMOSWorks 2006–2007. Inzhenerny analiz metodom konechnykh elementov*. Moscow, 784.
12. Alyamovskiy, A. A. (2010). *COSMOSWorks. Osnovy rascheta konstruktsiy na prochnost' v srede SolidWorks*. Moscow, 785.

13. Lovskaya, A. (2015). Computer simulation of wagon body bearing structure dynamics during transportation by train ferry. Eastern-European Journal of Enterprise Technologies, 3 (7 (75)), 9–14. doi: <https://doi.org/10.15587/1729-4061.2015.43749>
14. Fomin, O., Gerlici, J., Lovska, A., Kravchenko, K., Prokopenko, P., Fomina, A., Hauser, V. (2019). Durability Determination of the Bearing Structure of an Open Freight Wagon Body Made of Round Pipes during its Transportation on the Railway Ferry. Communications - Scientific Letters of the University of Zilina, 21 (1), 28–34.
15. DSTU 7598:2014. Vahony vantazhni. Zahalni vymohy do rozrakhunkiv ta proektuvannia novykh i modernizovanykh vahoniv koliyi 1520 mm (nesamokhidnykh) (2015). Kyiv, 162.
16. GOST 33211-2014. Vagony gruzovye. Trebovaniya k prochnosti dinamicheskim kachestvam (2016). Moscow, 54.
17. EN 12663-2. Railway applications – structural requirements of railway vehicle bodies – Part 2: Freight wagons (2010). BSI, 54. doi: <https://doi.org/10.3403/30152552u>
18. Bogomaz, G. I., Mehov, D. D., Pilipchenko, O. P., Chernomashentseva, Yu. G. (1992). Nagruzhenost' konteynerov-tsistern, raspolozhennyh na zheleznodorozhnoy platforme, pri udarах v avtostsepku. Dynamika ta keruvannia rukhom mekhanichnykh system, 87–95.
19. Kelrykh, M., Fomin, O. (2014). Perspective directions of planning carrying systems of gondolas. Metallurgical and Mining Industry, 6, 64–67.
20. Fomin, O. (2014). Modern requirements to carrying systems of railway general-purpose gondola cars. Metallurgical and Mining Industry, 5, 40–44.
21. Kondratiev, A. V., Gaidachuk, V. E., Kharchenko, M. E. (2019). Relationships Between the Ultimate Strengths of Polymer Composites in Static Bending, Compression, and Tension. Mechanics of Composite Materials, 55 (2), 259–266. doi: <https://doi.org/10.1007/s11029-019-09808-x>
22. Lovska, A. (2018). Simulation of Loads on the Carrying Structure of an Articulated Flat Car in Combined Transportation. International Journal of Engineering & Technology, 7 (4.3), 140–146. doi: <https://doi.org/10.14419/ijet.v7i4.3.19724>
23. Domin, Yu. V., Cherniak, H. Yu. (2003). Osnovy dynamiky vahoniv. Kyiv: KUETT, 269.