

## ABSTRACT AND REFERENCES

## APPLIED PHYSICS

**DOI: 10.15587/1729-4061.2020.206114****DEVELOPMENT OF A METHOD FOR DETERMINING THE WEAR OF ARTILLERY BARRELS BY ACOUSTIC FIELDS OF SHOTS (p. 6–18)****Yevhenii Dobrynin**National University "Odessa Maritime Academy",  
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A possibility of assessing the level of wear of artillery barrels by acoustic fields of shots was studied. Despite the importance of knowledge on the current barrel state, existing methods of wear assessment are not sufficiently prompt. These methods give rather rough estimates of wear or require expensive equipment. Unlike the known methods, the method proposed in the article is prompt, does not require large expenses, can be combined with a training firing, and is easily automated. Characteristics of the shock and muzzle waves generated by a gunshot were studied and differences in their parameters for barrels without wear and those with a critical wear level were shown. Initial shell velocity serves as a criterion indicator of wear. It was shown that according to the acoustic characteristics, a shot from the barrel having any degree of wear is equivalent to a shot from a gun of a smaller caliber. A computational experiment was conducted on real acoustic signals recorded during the firing of a 155 mm howitzer. Informative attributes of acoustic signals from shots were selected. They make it possible to automatically classify barrels into two classes: barrels suitable for use and barrels with wear exceeding the critical level. It was shown that the application of the support vector method (SVM) makes it possible to confidently classify barrels by the level of their wear based on the temporal and spectral attributes of the shock and muzzle waves. A cumulative analysis of spectral characteristics was used in the analysis of acoustic signals from shots. This has a significantly increased likelihood of correct barrel classification. The results are useful for practical use in artillery units in the field conditions. The study results enable the development of an automated system for assessing the barrel condition with high promptness. This ensures sufficient accuracy in assessing the level of barrel wear in the combat practice.

**Keywords:** artillery barrel wear, initial shell velocity, shock wave, muzzle wave.

**References**

1. Zakamennyy, I., Kucherova, V. G., Chervontseva, S. E. (Eds.) (2017). Proektirovanie spetsmashin, Ch. 1, Kn. 1. Artilleriyskie stvoly. Volgograd, 396.
2. Pushkarev, A. M. (2018). Elementy teorii iznosa artilleriyskih stvolov. V Vserossiyskaya nauchno-prakticheskaya konferentsiya «Kalashnikovskie chteniya». Izhevsk, 87–92.
3. Li, X., Mu, L., Zang, Y., Qin, Q. (2020). Study on performance degradation and failure analysis of machine gun barrel. Defence Technology, 16 (2), 362–373. doi: <https://doi.org/10.1016/j.dt.2019.05.008>
4. Banerjee, A., Nayak, N., Giri, D., Bandha, K. (2019). Effect of Gun Barrel Wear on Muzzle Velocity of a typical Artillery Shell. 2019 International Conference on Range Technology (ICORT). doi: <https://doi.org/10.1109/icort46471.2019.9069641>
5. Maciąg, P., Chałko, L. (2019). Use of sound spectral signals analysis to assess the technical condition of mechanical devices. MATEC Web of Conferences, 290, 01006. doi: <https://doi.org/10.1051/matecconf/201929001006>
6. Zhitnik, V. E., Petrenko, V. N., Trofimenko, P. E., Gridin, V. I. (2011). Calculation of conditions of the departure of the shell from the trunks canal by means of ballistic station. Systemy ozbrojeniya i viyskova tekhnika, 2 (26), 49–52.
7. Pinezich, J. D., Heller, J., Lu, T. (2010). Ballistic Projectile Tracking Using CW Doppler Radar. IEEE Transactions on Aerospace and Electronic Systems, 46 (3), 1302–1311. doi: <https://doi.org/10.1109/taes.2010.5545190>
8. Ka, M.-H., Vazhenin, N. A., Baskakov, A. I., Oh, C.-G. (2005). Analysis of Power Performance of a Muzzle Velocity Radar. 2005 5th International Conference on Information Communications & Signal Processing. doi: <https://doi.org/10.1109/icics.2005.1689038>
9. Zubkov, A. N., Kashin, S. V., Leshchenko, S. I., Lob, Ya. D., Martyugov, S. A., Naumets, N. A. et. al. (2009). Artilleriyskaya ballisticheskaya stantsiya novogo pokoleniya. Artilleriyskoe i strelkovoe vooruzhenie, 4, 15–18.
10. Budaretskiy, Y. I. (2015). Ways to increase the firing from cannons with the significant depreciation of the barrel. Systems of Arms and Military Equipment, 2 (42), 7–9.
11. Pushkaryov, A. M., Vershinin, A. A., Volf, I. G. (2015). Estimation of artillery barrel wear. Izvestiya Tul'skogo gosudarstvennogo universiteta. Tekhnicheskie nauki, 12 (1), 242–248.
12. Alchinov, V. I., Sidorov, L. I., Chistova, G. K. (2019). Nadezhnost' tehnicheskikh sistem voennogo naznacheniya. Moscow: Infra-Inzheneriya, 324.
13. Jain, J., Soni, S., Sharma, D. (2011). Determination of Wear Rate Equation and Estimation of Residual Life of 155mm Autofretted Gun Barrel. The International Journal of Multiphysics, 5 (1), 1–8. doi: <https://doi.org/10.1260/1750-9548.5.1.1>
14. Tsybulyak, B. (2016). Parameters degradation barrel artillery equipment during exploitation. Viyskovo-tehnichnyi zbirnyk, 14, 121–126.
15. Jankovych, R., Beer, S. (2011). T-72 tank barrel bore wear. International journal of mechanics, 5 (4), 353–360. Available at: <http://www.nauk.org/main/NAUN/mechanics/17-292.pdf>
16. Goncharenko, P. D., Haykov, V. L. (2012). Sovremennye sredstva kontrolya iznosa kanala orudiynogo stvola. Zbirnyk naukovykh prats akademiy viiskovo-morskykh syl im. P. S. Nakhimova, 1 (9), 22–30.
17. Haykov, V. L. (2013). Development of instrumental control methods and visualization of a gun barrels condition. Eastern-European Journal of Enterprise Technologies, 3 (7 (63)), 52–56. Available at: <http://journals.uran.ua/eejet/article/view/14825/12627>
18. Zheng, D., Tan, H., Zhou, F. (2017). A design of endoscopic imaging system for hyper long pipeline based on wheeled pipe robot. AIP Conference Proceedings, 1820, 060001. doi: <https://doi.org/10.1063/1.4977316>

19. Sokolov, A. V., Nasedkin, V. I., Kryuchkov, P. A., Naumov, D. N., Savinyyh, S. A., Nikitin, I. S., Devyatkin, V. A. (2014). Optiko-elektronnaya sistema kontrolya iznosa kanalov stvolov. Oboronaya tehnika, 10, 20–25.
20. Suh, K. (2018). A design on robot system for artillery barrel inspection. International Journal of Pure and Applied Mathematics, 118 (19), 1835–1844. Available at: <https://acadpubl.eu/jsi/2018-118-19/articles/19b/21.pdf>
21. Slutsky, V. E., Zaycev, A. A. (2014). On procedures of handling the ballistic preparation of artillery systems by applying the equipment of the check & test vehicle. Trudy Nizhegorodskogo gosudarstvennogo tehnicheskogo universiteta im. R.E. Alekseeva, 5 (107), 160–165.
22. Chang, H., Wu, Y.-C., Tsung, T.-T. (2011). Characteristics and measurement of supersonic projectile shock waves by a 32-microphone ring array. Review of Scientific Instruments, 82 (8), 084902. doi: <https://doi.org/10.1063/1.3622044>
23. Guo, S., Ma, Q., Zhou, X., Shao, R. (2012). Acoustic Recognition of Artillery Projectiles by SVM. Lecture Notes in Electrical Engineering, 345–351. doi: [https://doi.org/10.1007/978-3-642-25781-0\\_52](https://doi.org/10.1007/978-3-642-25781-0_52)
24. Dagallier, A., Cheinet, S., Cosnefroy, M., Rickert, W., Weßling, T., Wey, P., Juvé, D. (2019). Long-range acoustic localization of artillery shots using distributed synchronous acoustic sensors. The Journal of the Acoustical Society of America, 146 (6), 4860–4872. doi: <https://doi.org/10.1121/1.5138927>
25. Damarla, T. (2015). Battlefield Acoustics. Springer. doi: <https://doi.org/10.1007/978-3-319-16036-8>
26. Akman, Ç. (2017). Multi shooter Localization with Acoustic Sensors. Available at: <http://etd.lib.metu.edu.tr/upload/12621435/index.pdf>
27. Mäkinen, T., Pertila, P., Auranen, P. (2009). Supersonic bullet state estimation using particle filtering. 2009 IEEE International Conference on Signal and Image Processing Applications. doi: <https://doi.org/10.1109/icsipa.2009.5478625>
28. Sergienko, A. B. (2011). Tsifrovaya obrabotka signalov. Sankt-Peterburg: BHV-Peterburg, 768.
29. Zhao, X. Y., Zhou, K. D., He, L., Lu, Y., Wang, J., Zheng, Q. (2019). Numerical Simulation and Experiment on Impulse Noise in a Small Caliber Rifle with Muzzle Brake. Shock and Vibration, 2019, 1–12. doi: <https://doi.org/10.1155/2019/5938034>
30. Maher, R. C., Shaw, S. R. (2008). Deciphering gunshot recordings. 33rd International Conference: Audio Forensics-Theory and Practice. Available at: <http://www.aes.org/e-lib/browse.cfm?elib=14410>
31. Naz, P., Marty, C. (2006). Sound detection and localization of small arms, mortars, and artillery guns. Unattended Ground, Sea, and Air Sensor Technologies and Applications VIII. doi: <https://doi.org/10.1117/12.672936>
32. Rabinovich, E. V., Filipenko, N. Y., Shefel, G. S. (2018). Generalized model of seismic pulse. Journal of Physics: Conference Series, 1015, 052025. doi: <https://doi.org/10.1088/1742-6596/1015/5/052025>
33. ISO 9613-1:1993. Acoustics – Attenuation of sound during propagation outdoors – Part 1: Calculation of the absorption of sound by the atmosphere (1993). ISO, 26.
34. Bykov, A. P., Medvetskiy, S. V. (2010). K voprosu o koeffitsientah, harakterizuyushchih vnutriballisticheskij protsess klassicheskogo artilleriyskogo vystrela. Izvestiya Rossijskoy akademii raketynh i artillerijskikh nauk, 2 (64), 75–80.
35. Huseby, M. (2007). Noise emission data for M109, 155 mm field howitzer. Norwegian Defence Research Establishment (FFI), 45. Available at: <https://publications.ffi.no/nb/item/asset/dspace:3388/07-02530.pdf>
36. Field Artillery Sound Ranging and Flash Ranging (1979). United States. Department of the Army, Headquarters, 231. Available at: [https://books.google.com.ua/books/about/Field\\_Artillery\\_Sound\\_Ranging\\_and\\_Flash.html?id=0IhyEWUhBCsC&redir\\_esc=y](https://books.google.com.ua/books/about/Field_Artillery_Sound_Ranging_and_Flash.html?id=0IhyEWUhBCsC&redir_esc=y)
37. Loucks, R. B., Davis, B. S., Moss, L. G., Pham, T., Fong, M. (1995). A Method of Identifying Supersonic Projectiles Using Acoustic Signatures. USA ARL, 223. Available at: <https://apps.dtic.mil/dtic/tr/fulltext/u2/a299215.pdf>
38. Belov, V. V., Burkhatovskaya, Yu. B., Krasnenko, N. P., Rakov, A. S., Rakov, D. S., Shamanaeva, L. G. (2018). Experimental and theoretical investigations of near-ground acoustic radiation propagation in the atmosphere. Atmospheric and Oceanic Optics, 5, 372–377. doi: <https://doi.org/10.15372/aoo20180506>
39. Hacıhabiboglu, H. (2017). Procedural Synthesis of Gunshot Sounds Based on Physically Motivated Models. Game Dynamics, 47–69. doi: [https://doi.org/10.1007/978-3-319-53088-8\\_4](https://doi.org/10.1007/978-3-319-53088-8_4)
40. Wilson, D. K., White, M. J. (2010). Discrimination of Wind Noise and Sound Waves by Their Contrasting Spatial and Temporal Properties. Acta Acustica United with Acustica, 96 (6), 991–1002. doi: <https://doi.org/10.3813/aaa.918362>
41. Becker, G., Güdesen, A. (2000). Passive sensing with acoustics on the battlefield. Applied Acoustics, 59 (2), 149–178. doi: [https://doi.org/10.1016/s0003-682x\(99\)00023-7](https://doi.org/10.1016/s0003-682x(99)00023-7)
42. Dutoit, T., Marqués, F. (2009). Applied Signal Processing. A MATLAB™-Based Proof of Concept. Springer. doi: <https://doi.org/10.1007/978-0-387-74535-0>
43. Kirsanov, E. A., Sirota, A. A. (2012). Obrabotka informatsii v prostranstvenno-raspredelennyh sistemah radiomonitoringa: statisticheskiy i neyrosetevoy podhody. Moscow: Fizmatlit, 344.
44. Al-Jasri, G. Kh. M., Boltenkov, V. A., Chervonenko, P. P. (2016). Algoritms of cooperative heat trasfer leak detection in acoustic sensor nework. Elektrotehnichni ta kompiuterni systemy, 21 (97), 92–97.
45. Awad, M., Khanna, R. (2015). Support Vector Machines for Classification. Efficient Learning Machines, 39–66. doi: [https://doi.org/10.1007/978-1-4302-5990-9\\_3](https://doi.org/10.1007/978-1-4302-5990-9_3)
46. Wang, L. (2005). Support Vector Machines: Theory and Applications. Springer. doi: <https://doi.org/10.1007/b95439>
47. Temko, A., Nadeu, C. (2006). Classification of acoustic events using SVM-based clustering schemes. Pattern Recognition, 39 (4), 682–694. doi: <https://doi.org/10.1016/j.patcog.2005.11.005>
48. Häggele, D., Schefczik, F. (2018). Higher-order moments, cumulants, and spectra of continuous quantum noise measurements. Physical Review B, 98 (20). doi: <https://doi.org/10.1103/physrevb.98.205143>
49. Antoni, J., Randall, R. B. (2006). The spectral kurtosis: application to the vibratory surveillance and diagnostics of rotating machines. Mechanical Systems and Signal Processing, 20 (2), 308–331. doi: <https://doi.org/10.1016/j.ymssp.2004.09.002>
50. Hixon, T. J., Weismer, G., Hoit, J. D. (2014). Preclinical speech science: Anatomy, physiology, acoustics, perception. Plural Publishing. Available at: <https://psycnet.apa.org/record/2013-10861-000>
51. Demidova, L. A., Sokolova, Y. S. (2017). Two-stage data classification method based on SVM-algorithm and the k nearest neighbors algorithm. Vestnik of Ryazan State Radio Engineering University, 62, 119–132. doi: <https://doi.org/10.21667/1995-4565-2017-62-4-119-132>
52. Algazinov, E. K., Dryuchenko, M. A., Minakov, D. A., Sirota, A. A., Shulgin, V. A. (2013). Methods pattern recognition elements of cereal mixes of results spectral characteristics in the separation system real time. Vestnik Voronezhskogo gosudarstvennogo uni-

versiteta. Seriya: Sistemniy analiz i informatsionnye tehnologii, 2, 9–19.

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**DEVELOPMENT OF A SYSTEM FOR DETERMINING THE INFORMATIVENESS OF THE DIAGNOSING PARAMETERS FOR A CYLINDERPISTON GROUP IN THE DIESEL ENGINE DURING OPERATION (p. 19–29)**

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A possibility has been investigated to diagnose the condition of a cylinder-piston group in the diesel engine KamAZ-740.63-400 for trucks KamAZ-6460 after a 60,000 km run. The following diagnosing parameters have been selected: a crankcase gas pressure, the compression and vacuometric properties of a cylinder-piston group. A special feature of these mated parts is that they maintain the normal combustion process in the diesel engine cylinders, as well as its resource. We have determined the boundary limits for diagnosing a crankcase gas pressure – 2.39–2.41 KPa. Based on data about the crankcase gas pressure, the examined trucks revealed malfunctions on the runs of 36,000 km, 48,000 km, 60,000 km. Given the rules for assessing the characteristics of compression-related faults, the minimum compression value for the diesel engines was 30.05 MPa or its difference among the cylinders did not exceed 10–12 %. The data on compression helped detect faults after 48,000 km run and 60,000 km run. We have determined the boundaries of wear based on the vacuometric parameters: maximum vacuum – 69–86 KPa; residual vacuum – 26–41 KPa. Control of the vacuometric properties of a cylinder-piston group has revealed faults in the diesel engines over their run interval of 36,000–60,000 km.

An entropy approach has been applied to estimate the informativeness of the appropriate diagnosing parameters in bits. The

informativeness level of a crankcase gas pressure is 0.329 bits, compression in cylinders – 0.249 bits, vacuometric indicators – 0.582 bits.

This study allows the rational formation of the diesel engine condition diagnosing complexes during technical operation, as well determining the prerequisites for malfunctions. The data acquired are important for transportation and service enterprises and companies that manage freight vehicles.

**Keywords:** diesel engine, diagnosing, compression, cylinder-piston group, crankcase gas pressure, vacuometric properties of mated parts, entropy, informativeness.

**Reference**

1. Aulin, V., Hrynkiv, A., Lysenko, S., Dykha, A., Zamota, T., Dzyura, V. (2019). Exploring a possibility to control the stressed-strained state of cylinder liners in diesel engines by the tribotechnology of alignment. Eastern-European Journal of Enterprise Technologies, 3 (12 (99)), 6–16. doi: <https://doi.org/10.15587/1729-4061.2019.171619>
2. Kryshtopa, S., Melnyk, V., Dolishnii, B., Korohodskyi, V., Prunko, I., Kryshtopa, L. et. al. (2019). Improvement of the model of forecasting heavy metals of exhaust gases of motor vehicles in the soil. Eastern-European Journal of Enterprise Technologies, 4 (10 (100)), 44–51. doi: <https://doi.org/10.15587/1729-4061.2019.175892>
3. Marchenko, D. D., Dykha, A. V., Artyukh, V. A., Matvyeyeva, K. S. (2020). Studying the Tribological Properties of Parts Hardened by Rollers during Stabilization of the Operating Rolling Force. Journal of Friction and Wear, 41 (1), 58–64. doi: <https://doi.org/10.3103/s1068366620010122>
4. Koszałka, G. (2014). Model of operational changes in the combustion chamber tightness of a diesel engine. Eksplotacjja i Niezawodnosć, 16 (1), 133–139. Available at: <https://www.scopus.com/inward/record.uri?eid=2-s2.0-84891610623&partnerID=40&md5=1c43eddaf5a3d994ebf7d6d2df41a221>
5. Aulin, V., Hrynkiv, A., Lyashuk, O., Vovk, Y., Lysenko, S., Holub, D. et. al. (2020). Increasing the Functioning Efficiency of the Working Warehouse of the “UVK Ukraine” Company Transport and Logistics Center. Communications - Scientific Letters of the University of Zilina, 22 (2), 3–14. doi: <https://doi.org/10.26552/com.c.2020.2.3-14>
6. Shramenko, N., Pavlenko, O., Muzylyov, D. (2019). Information and communication technology: Case of using petri nets for grain delivery simulation at logistics system. CEUR Workshop Proceedings, 2353, 935–949. Available at: <https://www.scopus.com/inward/record.uri?eid=2-s2.0-85065480575&partnerID=40&md5=a53346ecdc4ad9fe63fb12c25b5c32>
7. Aulin, V., Lyashuk, O., Pavlenko, O., Velykodnyi, D., Hrynkiv, A., Lysenko, S. et. al. (2019). Realization of the logistic approach in the international cargo delivery system. Communications - Scientific Letters of the University of Zilina, 21 (2), 3–12. Available at: <https://www.scopus.com/inward/record.uri?eid=2-s2.0-85066994460&partnerID=40&md5=105d35bd46f8ab7b6de0b6688948d0e3>
8. Osadchiy, S. I., Zozulya, V. A. (2013). Combined Method for the Synthesis of Optimal Stabilization Systems of Multidimensional Moving Objects under Stationary Random Impacts. Journal of Automation and Information Sciences, 45 (6), 25–35. doi: <https://doi.org/10.1615/jautomatinfscien.v45.i6.30>
9. Kryshtopa, S., Panchuk, M., Kozak, F., Dolishnii, B., Mykytii, I., Skalatska, O. (2018). Fuel economy raising of alternative fuel converted diesel engines. Eastern-European Journal of Enterprise Technologies, 4 (8 (94)), 6–13. doi: <https://doi.org/10.15587/1729-4061.2018.139358>

10. Aulin, V., Lysenko, S., Lyashuk, O., Hrinkiv, A., Velykodnyi, D., Vovk, Y. et. al. (2019). Wear Resistance Increase of Samples Tribomating in Oil Composite with Geo Modifier KGMF-1. *Tribology in Industry*, 41 (2), 156–165. doi: <https://doi.org/10.24874/ti.2019.41.02.02>
11. Aulin, V. V., Pankov, A. O., Zamota, T. M., Lyashuk, O. L., Hrynkiv, A. V., Tykhyi, A. A., Kuzyk, A. V. (2019). Development of mechatronic module for the seeding control system. *INMATEH - Agricultural Engineering*, 59 (3), 181–188. doi: <https://doi.org/10.35633/inmateh-59-20>
12. Ivashkiv, I., Kupalova, H., Goncharenko, N., Khrutba, Y., Vovk, I. (2019). Optimization of commodity flows: The case of bakery enterprises of Ukraine. *Montenegrin Journal of Economics*, 15 (3), 205–216. doi: <https://doi.org/10.14254/1800-5845/2019.15-3.15>
13. Kryshtopa, S. I., Prun'ko, I. B., Dolishnii, B. V., Panchuk, M. V., Bogatchuk, I. M., Mel'nyk, V. M. (2019). Regularities of Wear of Metal-Polymer Friction Couples Under the Influence of Tribocurrents. *Materials Science*, 55 (2), 193–200. doi: <https://doi.org/10.1007/s11003-019-00288-x>
14. Aulin, V., Derkach, O., Makarenko, D., Hrynkiv, A., Pankov, A., Tykhyi, A. (2019). Analysis of tribological efficiency of movable junctions “polymericcomposite materials – steel.” *Eastern-European Journal of Enterprise Technologies*, 4 (12 (100)), 6–15. doi: <https://doi.org/10.15587/1729-4061.2019.176845>
15. Dykha, A., Marchenko, D., Artyukh, V., Zubiekhina-Khaiiat, O., Kurepin, V. (2018). Study and development of the technology for hardening rope blocks by reeling. *Eastern-European Journal of Enterprise Technologies*, 2 (1 (92)), 22–32. doi: <https://doi.org/10.15587/1729-4061.2018.126196>
16. Aulin, V., Hrynkiv, A., Lysenko, S., Rohovskii, I., Chernovol, M., Lyashuk, O., Zamota, T. (2019). Studying truck transmission oils using the method of thermal-oxidative stability during vehicle operation. *Eastern-European Journal of Enterprise Technologies*, 1 (6 (97)), 6–12. doi: <https://doi.org/10.15587/1729-4061.2019.156150>
17. Ageev, E. V., Altukhov, A. Y., Scherbakov, A. V., Novikov, A. N. (2017). Informativeness increasing of internal combustion engines diagnosis due to technical endoscope. *Journal of Engineering and Applied Sciences*, 12 (4), 1028–1030. Available at: <https://www.scopus.com/inward/record.uri?eid=2-s2.0-85018945495&doi=10.3923%2fjeasci.2017.1028.1030&partnerID=40&md5=b0d5548616d81ce16fd58c7143301f98>
18. Bulgakov, V., Ivanovs, S., Safchenko, I., Boris, A., Rychlivskyj, P. (2019). Theoretical Research of the Design and Technological Parameters of a Device for Lifting of Deep-Seated Table Root Crops. *Acta Technologica Agriculturae*, 22 (3), 99–103. doi: <https://doi.org/10.2478/ata-2019-0018>
19. Aulin, V. V., Chernovol, M. I., Pankov, A. O., Zamota, T. M., Panayotov, K. K. (2017). Sowing machines and systems based on the elements of fluidics. *INMATEH - Agricultural Engineering*, 53 (3), 21–28. Available at: <https://www.scopus.com/inward/record.uri?eid=2-s2.0-85039172369&partnerID=40&md5=248069fc8914b34091c229527a0cc3e>
20. Hevko, R. B., Strishenets, O. M., Lyashuk, O. L., Tkachenko, I. G., Klendii, O. M., Dzyura, V. O. (2018). Development of a pneumatic screw conveyor design and substantiation of its parameters. *INMATEH - Agricultural Engineering*, 54 (1), 153–160. Available at: <https://www.scopus.com/inward/record.uri?eid=2-s2.0-85053484099&partnerID=40&md5=5bdd8ec973095080f9afe89de7494f9c>
21. Kryshtopa, S., Kryshtopa, L., Melnyk, V., Dolishnii, B., Prun'ko, I., Demianchuk, Y. (2017). Experimental research on diesel engine working on a mixture of diesel fuel and fusel oils. *Transport Problems*, 12 (2), 53–63. doi: <https://doi.org/10.20858/tp.2017.12.2.6>
22. Kabat, O. S., Kharchenko, B. G., Derkach, O. D., Artemchuk, V. V., Babenko, V. G. (2019). Polymer composites based on fluoroplastic and method for the production thereof. *Voprosy Khimii i Khimicheskoi Tekhnologii*, 2019 (3), 116–122. doi: <https://doi.org/10.32434/0321-4095-2019-124-3-116-122>
23. Kobets, A. S., Derkach, O. D., Kabat, O. S., Kovalenko, V. L., Kotok, V. A. (2019). Recycling of constructional plastics with additives of exhausted polyethylene. *ARPN Journal of Engineering and Applied Sciences*, 14 (13), 2397–2406. Available at: <https://www.scopus.com/inward/record.uri?eid=2-s2.0-85076533661&partnerID=40&md5=2017ef4ab03e1c372dedc7b6f49f24a2>
24. Aulin, V., Lyashuk, O., Hrynkiv, A., Lysenko, S., Zamota, T., Vovk, Y. et. al. (2019). Determination of the Rational Composition of the Additive to Oil with the Use of the Katerynivka Friction Geo Modifier. *Tribology in Industry*, 41 (4), 548–562. doi: <https://doi.org/10.24874/ti.2019.41.04.08>
25. Aulin, V., Hrynkiv, A., Lysenko, S., Zamota, T., Pankov, A., Tykhyi, A. (2019). Determining the rational composition of tribologically active additive to oil to improve characteristics of tribosystems. *Eastern-European Journal of Enterprise Technologies*, 6 (12 (102)), 52–64. doi: <https://doi.org/10.15587/1729-4061.2019.184496>
26. Dykha, A., Sorokatyti, R., Makovkin, O., Babak, O. (2017). Calculation-experimental modeling of wear of cylindrical sliding bearings. *Eastern-European Journal of Enterprise Technologies*, 5 (1 (89)), 51–59. doi: <https://doi.org/10.15587/1729-4061.2017.109638>
27. Svazas, M., Navickas, V., Krajnakova, E., Nakonieczny, J. (2019). Sustainable supply chain of the biomass cluster as a factor for preservation and enhancement of forests. *Journal of International Studies*, 12 (2), 309–321. doi: <https://doi.org/10.14254/2071-8330.2019/12-2/20>
28. Dykha, A. V., Zaspa, Y. P., Slashchuk, V. O. (2018). Triboaoustic Control of Fretting. *Journal of Friction and Wear*, 39 (2), 169–172. doi: <https://doi.org/10.3103/s1068366618020046>
29. Ropyak, L. Y., Shatskyi, I. P., Makoviichuk, M. V. (2017). Influence of the Oxide-Layer Thickness on the Ceramic-Aluminium Coating Resistance to Indentation. *Metallofizika i Noveishie Tekhnologii*, 39 (4), 517–524. doi: <https://doi.org/10.15407/mfint.39.04.0517>
30. Aleksandr, D., Dmitry, M. (2018). Prediction the wear of sliding bearings. *International Journal of Engineering & Technology*, 7 (2.23), 4–8. doi: <https://doi.org/10.14419/ijet.v7i2.23.11872>
31. Aulin, V., Hrynkiv, A., Lysenko, S., Lyashuk, O., Zamota, T., Holub, D. (2019). Studying the tribological properties of mated materials C61900 - A48-25BC1.25B№. 25 in composite oils containing geomodifiers. *Eastern-European Journal of Enterprise Technologies*, 5 (12 (101)), 38–47. doi: <https://doi.org/10.15587/1729-4061.2019.179900>
32. Sorokatyti, R., Chernets, M., Dykha, A., Mikosyanchyk, O. (2019). Phenomenological Model of Accumulation of Fatigue Tribological Damage in the Surface Layer of Materials. *Mechanisms and Machine Science*, 73, 3761–3769. doi: [https://doi.org/10.1007/978-3-030-20131-9\\_371](https://doi.org/10.1007/978-3-030-20131-9_371)
33. Prokopenko, A. K., Golubev, A. P., Korneev, A. A. (2019). Research on Wear Resistance of Multifunctional Coatings Used in the Manufacture of Art and Industrial Products. *Materials Science Forum*, 945, 670–674. doi: <https://doi.org/10.4028/www.scientific.net/msf.945.670>
34. Kazmierczak, A. (2008). Physical aspects of wear of the piston-ring – cylinder set of combustion engines. *Proceedings of*

- the Institution of Mechanical Engineers, Part D: Journal of Automobile Engineering, 222 (11), 2103–2119. doi: <https://doi.org/10.1243/09544070jauto877>
35. Dykha, A. V., Kuzmenko, A. G. (2016). Distribution of friction tangential stresses in the Courtney-Pratt experiment under Bowden's theory. *Journal of Friction and Wear*, 37 (4), 315–319. doi: <https://doi.org/10.3103/s1068366616040061>
  36. Kishortal, D. B., Mukhopadhyay, A. K. (2016). Failure mode effective analysis of diesel engines used in dumpers. *Journal of Mines, Metals and Fuels*, 64 (11), 564–567. Available at: <https://www.scopus.com/inward/record.uri?eid=2-s2.0-85019202283&partnerID=40&md5=5cde424e70d62b24c7bf014d3832dc1e>
  37. Jones, N. B., Li, Y.-H. (2000). A review of condition monitoring and fault diagnosis for diesel engines. *Tribotest*, 6 (3), 267–291. doi: <https://doi.org/10.1002/tt.3020060305>

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## ANALYTICAL AND PHYSICAL MODELING OF THE MAGNETICALLY ACTIVE PART OF A LINEAR ELECTRIC GENERATOR WITH PERMANENT MAGNETS (p. 30–37)

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Linear electric generators are increasingly used in autonomous systems that require a compact source of electricity and when it is necessary to simplify mechanisms of power systems. To study the characteristics of a linear electric generator, an analytical model of its magnetically active part was proposed. The model is based on the assumption of the periodicity of linear translational motion of the armature relative to the stationary cylindrical winding. Based on the representation of the magnetic field of the generator's armature by cylindrical harmonics of the scalar potential, the magnetic flux generated by the inductor was analyzed. The inductor design contains several pairwise oppositely oriented cylindrical permanent magnets. The use of representations based on cylindrical harmonics for the magnetic flux and EMF induced in a circular circuit has made it possible to substantiate the rational number of cylindrical armature magnets and their geometric parameters. The losses caused by the technological necessity of using annular magnets instead of solid continuous cylindrical ones with the same overall dimensions were estimated. Analysis of losses of the magnetic flux linkage with the current winding resulting from the presence of technologically necessary clearance between the permanent magnets and the winding sections was carried out. An analysis of arrangement and switching of the winding sections was car-

ried out. It has made it possible to justify the choice of rational cross-sectional dimensions. For experimental verification of the analytically obtained results, a physical model of a linear electric generator with an armature containing permanent cylindrical magnets was designed. Its translational periodic movement was provided through an external electric drive. Analysis of the EMF dependences recorded with a digital oscilloscope with a small (5 %) error has confirmed the obtained analytical results and correctness of the theses underlying the model.

**Keywords:** linear electric generator, magnetic flux, permanent magnet, electromotive force, cylindrical harmonic.

## References

1. Kondratenko, I. P., Rashchepkin, A. P., Vashchyshyn, D. D. (2010). Rozrakhunok elektrorushyinoi sly liniynoho heneratora dlia peretvorennia enerhiyi khvyl. Visnyk Kremenchutskoho derzhavnoho universytetu im. M. Ostrohradskoho, 4 (1), 72–75.
2. Slynchenko, A. A., Klyuev, K. M. (2005). Sudovoy lineyniy dizel'-generator dlya propul'sivnyh kompleksov. Sudovye energeticheskie ustanovaiki, 12, 145–151.
3. Miao, Y., Zuo, Z., Feng, H., Guo, C., Song, Y., Jia, B., Guo, Y. (2016). Research on the Combustion Characteristics of a Free-Piston Gasoline Engine Linear Generator during the Stable Generating Process. Energies, 9 (8), 655. doi: <https://doi.org/10.3390/en9080655>
4. Menzhinski, A. B., Malashin, A. N., Sukhodolov, Y. V. (2019). Experimental Verification of the Adequacy of Mathematical Model of the Reciprocating Electric Electromagnetically Excited Generator. ENERGETIKA. Proceedings of CIS Higher Education Institutions and Power Engineering Associations, 62 (2), 168–176. doi: <https://doi.org/10.21122/1029-7448-2019-62-2-168-176>
5. Kondratenko, I. P., Rashchepkin, A. P., Vashchishin, D. D. (2012). A dynamic model of a linear permanent magnet generator for converting wave energy. Tekhnichna elektrodynamika, 2, 113–114. Available at: [http://techned.org.ua/2012\\_2/st54.pdf](http://techned.org.ua/2012_2/st54.pdf)
6. Mikalsen, R., Roskilly, A. P. (2007). A review of free-piston engine history and applications. Applied Thermal Engineering, 27 (14–15), 2339–2352. doi: <https://doi.org/10.1016/j.applthermaleng.2007.03.015>
7. Jia, B., Smallbone, A., Mikalsen, R., Shivaprasad, K. V., Roy, S., Roskilly, A. P. (2019). Performance Analysis of a Flexi-Fuel Turbine-Combined Free-Piston Engine Generator. Energies, 12 (14), 2657. doi: <https://doi.org/10.3390/en12142657>
8. Jia, B., Zuo, Z., Tian, G., Feng, H., Roskilly, A. P. (2015). Development and validation of a free-piston engine generator numerical model. Energy Conversion and Management, 91, 333–341. doi: <https://doi.org/10.1016/j.enconman.2014.11.054>
9. Kosaka, H., Akita, T., Moriya, K., Goto, S., Hotta, Y., Umeno, T., Nakakita, K. (2014). Development of Free Piston Engine Linear Generator System Part 1 - Investigation of Fundamental Characteristics. SAE Technical Paper Series. doi: <https://doi.org/10.4271/2014-01-1203>
10. Goto, S., Moriya, K., Kosaka, H., Akita, T., Hotta, Y., Umeno, T., Nakakita, K. (2014). Development of Free Piston Engine Linear Generator System Part 2 - Investigation of Control System for Generator. SAE Technical Paper Series. doi: <https://doi.org/10.4271/2014-01-1193>
11. Feng, H., Guo, C., Yuan, C., Guo, Y., Zuo, Z., Roskilly, A. P., Jia, B. (2016). Research on combustion process of a free piston diesel linear generator. Applied Energy, 161, 395–403. doi: <https://doi.org/10.1016/j.apenergy.2015.10.069>
12. Jia, B., Smallbone, A., Zuo, Z., Feng, H., Roskilly, A. P. (2016). Design and simulation of a two- or four-stroke free-piston engine

- generator for range extender applications. Energy Conversion and Management, 111, 289–298. doi: <https://doi.org/10.1016/j.enconman.2015.12.063>
13. Mikalsen, R., Roskilly, A. P. (2008). The design and simulation of a two-stroke free-piston compression ignition engine for electrical power generation. Applied Thermal Engineering, 28 (5-6), 589–600. doi: <https://doi.org/10.1016/j.applthermefleng.2007.04.009>
14. Jia, B., Tian, G., Feng, H., Zuo, Z., Roskilly, A. P. (2015). An experimental investigation into the starting process of free-piston engine generator. Applied Energy, 157, 798–804. doi: <https://doi.org/10.1016/j.apenergy.2015.02.065>
15. Jia, B., Smallbone, A., Feng, H., Tian, G., Zuo, Z., Roskilly, A. P. (2016). A fast response free-piston engine generator numerical model for control applications. Applied Energy, 162, 321–329. doi: <https://doi.org/10.1016/j.apenergy.2015.10.108>
16. Watson, G. N. (1922). A treatise on the theory of Bessel functions. Cambridge: Cambridge Univ. Press, 804. Available at: [https://www.forgottenbooks.com/de/download/ATreatiseontheTheoryofBesselFunctions\\_10019747.pdf](https://www.forgottenbooks.com/de/download/ATreatiseontheTheoryofBesselFunctions_10019747.pdf)
17. Smythe, W. (1950). Static and Dynamic Electricity. McGraw-Hill, 623. Available at: <https://archive.org/details/StaticAndDynamicElectricity/page/n95/mode/2up>
18. Gray, A., Mathews, G. B. (1895). A treatise on Bessel functions and their applications to physics. Macmillan and Co., 316. Available at: <https://archive.org/details/treatiseonbessel00grayuoft/page/n10/mode/2up>
19. Getman, A. V., Konstantinov, A. V. (2013). Cylindrical harmonics of magnetic field of linear magnetized cylinder. Tekhnichna elektrodynamika, 1, 3–8. Available at: [http://techned.org.ua/2013\\_1/st1.pdf](http://techned.org.ua/2013_1/st1.pdf)
20. Getman, A. V., Konstantinov, A. V. (2011). Cylindrical harmonics of magnetic field of a uniformly magnetized cylinder. Elektrotehnika i Elektromekhanika, 5, 51–53. Available at: [http://repository.kpi.kharkov.ua/bitstream/KhPI-Press/13573/1/EE\\_2011\\_5\\_Get%27man\\_Tsilindricheskiye.pdf](http://repository.kpi.kharkov.ua/bitstream/KhPI-Press/13573/1/EE_2011_5_Get%27man_Tsilindricheskiye.pdf)

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**THE STRESSED STRAINED STATE OF A ROD AT CRYSTALLIZATION CONSIDERING THE MUTUAL INFLUENCE OF TEMPERATURE AND MECHANICAL FIELDS (p. 38–49)**

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This paper reports a solution to the problem of determining the motion law of the crystallization front and the thermome-

chanical state of a two-phase rod for the case of mutual influence of the temperature and mechanical fields. An approximate analytical method has been used to solve the problem, combined with the method of successive intervals and a Gibbs variation principle. This method should indicate what is “more beneficial” to nature under the assigned external influences – to change the temperature of the fixed element of a body or to transfer this element from one aggregate state to another. It is this approach that has made it possible, through the defined motion law of an interphase boundary, to take into consideration the effect of temperature on the tense-deformed state in the body, and vice versa. The ratios have been obtained to define the motion law of an interphase boundary, the temperature field, and the tense-deformed state in the rod. The results are shown in the form of charts of temperature and stress dependence on time and a coordinate.

An analysis of the results shows that changes in the conditions of heat exchange with the environment and geometric dimensions exert a decisive influence on the crystallization process, and, consequently, on temperature and mechanical fields. The principal result is the constructed approximate analytical method and an algorithm for solving the problem on thermoviscoelasticity for growing bodies (bodies with a moving boundary) in the presence of a phase transition considering the heat exchange with the environment. Based on the method developed, the motion law of an interphase boundary, a temperature field, and the tense-deformed state are determined while solving the so-called quasi-related problem of thermoviscoelasticity. An approximate analytical solution has been obtained, which could be used by research and design organizations in modeling various technological processes in machine building, metallurgy, rocket and space technology, and construction.

**Keywords:** thermomechanical state, Gibbs variation principle, crystallization front, approximate analytical method.

**References**

1. Dron, M., Dreus, A., Golubek, A., Abramovsky, Y. (2018). Investigation of aerodynamics heating of space debris object at reentry to earth atmosphere. 69th International Astronautical Congress, IAC-18-A6.1.5. Bremen, 7.
2. Yemets, V., Harkness, P., Dron', M., Pashkov, A., Worrall, K., Middleton, M. (2018). Autophage Engines: Toward a Throttleable Solid Motor. Journal of Spacecraft and Rockets, 55 (4), 984–992. doi: <https://doi.org/10.2514/1.a34153>
3. Yemets, M., Yemets, V., Dron, M., Harkness, P., Worrall, K. (2018). Caseless throttleable solid motor for small Spacecraft. 69th International Astronautical Congress, IAC-18.C4.8-B4.5A.13. Bremen, 10.
4. Dreus, A. Y., Kozhevnykov, A. A., Liu, B., Sudakova, D. A. (2019). Approximate analytical model of rock thermal cyclical disintegration under convective cooling. Naukovyi Visnyk Natsionalnoho Hirnychoho Universytetu, 4, 42–47. doi: <https://doi.org/10.29202/nvngu/2019-4/5>
5. Opitz, F., Treffinger, P., Wöllenstein, J. (2017). Modeling of Radiative Heat Transfer in an Electric Arc Furnace. Metallurgical and Materials Transactions B, 48 (6), 3301–3315. doi: <https://doi.org/10.1007/s11663-017-1078-6>
6. Sudakov, A., Dreus, A., Ratov, B., Delikesheva, D. (2018). Theoretical bases of isolation technology for swallowing horizons using thermoplastic materials. News of the National Academy of Sciences of the Republic of Kazakhstan, Series of Geology and Technical Sciences, 2 (428), 72–80.
7. Syasev, A., Zelenskaya, T. (2015). Lengthwise movement dynamic boundary-value problem for trailing boundary ropes.

- Metallurgical and Mining Industry, 3, 283–287. Available at: [http://www.metaljournal.com.ua/assets/Journal/english-edition/MMI\\_2015\\_3/036%20Syasev.pdf](http://www.metaljournal.com.ua/assets/Journal/english-edition/MMI_2015_3/036%20Syasev.pdf)
8. Kravets, E. (2019). Determining the structure of a laminar detachable current in an open cavity. Eastern-European Journal of Enterprise Technologies, 6 (8 (102)), 28–37. doi: <https://doi.org/10.15587/1729-4061.2019.183811>
  9. Kozhevnikov, A. A., Sudakov, A. K., Dreus, A. Yu., Lysenko, Ye. Ye. (2014). Study of heat transfer in cryogenic gravel filter during its transportation along a drillhole. Naukovyi Visnyk Natsionalnoho Hirnychoho Universytetu, 6, 49–54.
  10. Kulikov, R. G., Kulikova, T. G. (2014). Numerical methods for solving the problem of polymer crystallizing media deformation taking into account finite deformations. Computational Continuum Mechanics, 7 (2), 172–180. doi: <https://doi.org/10.7242/1999-6691/2014.7.2.18>
  11. Kul'bovskiy, I. K., Karelin, S. V., Ilyushkin, D. A. (2008). Komp'yuternoe modelirovanie protsessov kristallizatsii massivnykh otlivok v tulosok tsilindrov sudovykh dizeley. Vestnik BGU, 2 (18), 16–19.
  12. Tkachuk, A. N. (2008). Issledovaniya termouprugih kontaktnykh zadach elementov press-form dlya lit'ya pod davleniem s uchetom fazovyh prevrashcheniy v otlivke. Vestnik NTU «KhPI», 2, 144–158.
  13. Senchenkov, I. K., Oksenchuk, N. D. (2013). An estimation of effects of thermostructural mechanical coupling under pulse loading of half-space. Bulletin of Taras Shevchenko National University of Kyiv Series: Physics & Mathematics, 3, 217–219.
  14. Bonetti, E., Frémond, M., Lexcellent, C. (2005). Global Existence and Uniqueness for a Thermomechanical Model for Shape Memory Alloys with Partition of the Strain. Mathematics and Mechanics of Solids, 11 (3), 251–275. doi: <https://doi.org/10.1177/1081286506040403>
  15. Rao, A., Srinivasa, A. R. (2014). A three-species model for simulating torsional response of shape memory alloy components using thermodynamic principles and discrete Preisach models. Mathematics and Mechanics of Solids, 20 (3), 345–372. doi: <https://doi.org/10.1177/1081286514545917>
  16. Holland, M. A., Kosmata, T., Goriely, A., Kuhl, E. (2013). On the mechanics of thin films and growing surfaces. Mathematics and Mechanics of Solids, 18 (6), 561–575. doi: <https://doi.org/10.1177/1081286513485776>
  17. Paroni, R., Tomassetti, G. (2017). Linear models for thin plates of polymer gels. Mathematics and Mechanics of Solids, 23 (5), 835–862. doi: <https://doi.org/10.1177/1081286517698740>
  18. Hossain, M., Chatzigeorgiou, G., Meraghni, F., Steinmann, P. (2015). A multi-scale approach to model the curing process in magneto-sensitive polymeric materials. International Journal of Solids and Structures, 69–70, 34–44. doi: <https://doi.org/10.1016/j.ijsolstr.2015.06.011>
  19. Carniel, T. A., Muñoz-Rojas, P. A., Vaz, M. (2015). A viscoelastic viscoplastic constitutive model including mechanical degradation: Uniaxial transient finite element formulation at finite strains and application to space truss structures. Applied Mathematical Modelling, 39 (5–6), 1725–1739. doi: <https://doi.org/10.1016/j.apm.2014.09.036>
  20. Hudramovich, V. S., Gart, É. L., Strunin, K. A. (2017). Modeling of the Behavior of Plane-Deformable Elastic Media with Elongated Elliptic and Rectangular Inclusions. Materials Science, 52 (6), 768–774. doi: <https://doi.org/10.1007/s11003-017-0020-z>
  21. Hart, E. L., Hudramovich, V. S. (2016). Projection-iterative modification of the method of local variations for problems with a quadratic functional. Journal of Applied Mathematics and Mechanics, 80 (2), 156–163. doi: <https://doi.org/10.1016/j.jappmathmech.2016.06.005>
  22. Hart, E. L., Hudramovich, V. S. (2014). Projection-Iterative Schemes for the Realization of the Finite-Element Method in Problems of Deformation of Plates with Holes and Inclusions. Journal of Mathematical Sciences, 203 (1), 55–69. doi: <https://doi.org/10.1007/s10958-014-2090-x>
  23. Lykov, A. V. (1967). Teoriya teploprovodnosti. Moscow: Vysshaya shkola, 560.
  24. Syasev, A. V. (2001). Priblizhennyi analiticheskiy metod rascheta rastushchih tel s uchetom fazovogo perehoda. Visnyk Dniproper. un-tu. Seriya: Mekhanika, 1 (5), 125–137.
  25. Karnauhov, V. G. (1982). Svyazannye zadachi termovyzkou-prugosti. Kyiv: Naukova dumka, 250.
  26. Lyubov, B. Ya. (1975). Teoriya kristallizatsii v bol'shih obemah. Moscow: Nauka, 256.
  27. Nikitenko, N. I. (1978). Issledovanie protsessov teplo-i masoobmena metodom setok. Kyiv: Naukova dumka, 213.
  28. Arutyunyan, N. H., Drozdov, A. D., Naumov, V. E. (1987). Mekhanika rastushchih vyazkouprugoplasticheskikh tel. Moscow: Nauka, 472.

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**FEATURES OF MATHEMATICAL MODELING OF ELECTROMAGNETIC PROCESSING OF BULK MATERIALS (p. 49–59)**

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The article notes the features of applying the general equations of mathematical physics of an elliptic type in problems of modeling specific phenomena of the interaction of electromagnetic fields with elements and particles of an inhomogeneous dispersed medium. Such phenomena take place in installations for the separation of organic and mineral raw materials or the electromagnetic treatment of grain, seeds, etc. This is relevant, because the usual approach to the formulation of mathematical models in these problems, which is mainly based on differential equations of field theory in a simplified form, does not always adequately reflect the physical essence of the mentioned phenomena. Therefore, it limits the possibilities of an in-depth study of the influence of many factors determining the final results of separation and electromagnetic processing (EMP)

processes. In the present work, an alternative approach is proposed based on the use of integral equations of field theory, which is based on the concept of primary and secondary field sources and can significantly reduce the order of the system of equations for the numerical implementation of algorithms for solving EMP problems, and the total amount of necessary computing resources. With this approach, local parameters of the field in interaction with individual particles and their influence on one another become available for calculation. This aspect is essential for determining the technological characteristics of EMP production installations. The presented mathematical model, in contrast to the common simplified approaches to determining the field parameters and ponderomotive forces acting on the particles of matter in the field, adequately reflects the physical laws of the distribution of potentials and electric field strength of real charges and induced sources. Due to this, it clearly reproduces the mechanism of the formation of the main components of mechanical forces acting on the polarized body from the side of the electric field as a whole, through the densities of elementary forces with which the field acts on surface charges induced in dielectric bodies in the field of action of the fields. Such a mathematical model is a universal and compact tool for analysis, design, and optimization of various installations and devices that use an electric field and its electromechanical interaction with the medium and individual bodies.

**Keywords:** electromagnetic treatment, dispersed materials, mathematical modeling, electric field, particles, substance, force.

## References

1. Kyurchev, S., Kolodiy, A. (2013). The analysis of existing separators which are using for the separation of the seed. Motrol. Commission of motorization and energetics in agriculture, 15, 2, 197–204.
2. Dascalescu, L., Dragan, C., Bilici, M., Beleca, R., Hemery, Y., Rouau, X. (2010). Electrostatic Basis for Separation of Wheat Bran Tissues. *IEEE Transactions on Industry Applications*, 46 (2), 659–665. doi: <https://doi.org/10.1109/tia.2010.2040050>
3. Tarushkin, V. I. (2007). Dielektricheskaya separatsiya semyan. Vol. 1. Moscow, 401.
4. Korko, V. S., Gorodetskaya, E. A. (2013). Elektrofizicheskie metody stimulyatsii rastitel'nyh obektov. Minsk: BGATU, 232.
5. Kozlov, A. P. (2007). Bifilyarnaya obmotka dielektricheskogo separatora dlya sortirovaniya semyan zernovyh kul'tur. Moscow, 197.
6. Mayer Laigle, C., Barakat, A. (2017). Electrostatic Separation as an Entry into Environmentally Eco-Friendly Dry Biorefining of Plant Materials. *Journal of Chemical Engineering & Process Technology*, 08 (04). doi: <https://doi.org/10.4172/2157-7048.1000354>
7. Karmazin, V. V., Karmazin, V. I. (2005). Magnitnye, elektricheskie i spetsial'nye metody obogashcheniya poleznyh is-kopayemyh. Vol. 1. Moscow: Izdatel'stvo Moskovskogo gosudarstvennogo gornogo universiteta, 669.
8. Salama, A., Richard, G., Medles, K., Zeghloul, T., Dascalescu, L. (2018). Distinct recovery of copper and aluminum from waste electric wires using a roll-type electrostatic separator. *Waste Management*, 76, 207–216. doi: <https://doi.org/10.1016/j.wasman.2018.03.036>
9. Tilmantine, A., Medles, K., Younes, M., Bendaoud, A., Dascalescu, L. (2010). Roll-Type Versus Free-Fall Electrostatic Separation of Tribocharged Plastic Particles. *IEEE Transactions on Industry Applications*, 46 (4), 1564–1569. doi: <https://doi.org/10.1109/tia.2010.2049553>
10. Matsusaka, S., Maruyama, H., Matsuyama, T., Ghadiri, M. (2010). Triboelectric charging of powders: A review. *Chemical Engineering Science*, 65 (22), 5781–5807. doi: <https://doi.org/10.1016/j.ces.2010.07.005>
11. Ali Ebrahim, S. (2017). Biological Effects of Magnetic Water on Human and Animals. *Biomedical Sciences*, 3 (4), 78. doi: <https://doi.org/10.11648/j.bs.20170304.12>
12. Malkin, E. S., Furtat, I. E., Pryimak, O. V. (2009). Metodyka rozrakhunku ustyanovok dlja pomikshennia ta ochyshchennia vody v elektrychnykh i mahnitnykh poliakh. Nova Tema, 2, 26–29.
13. Lerman, L. B., Grischuk, O. Yu., Shkoda, N. G., Shostak, S. V. (2012). Features of Interaction of an Electromagnetic Radiation with Small Particles and Their Ensembles: Theoretical Aspects. *Uspekhi fiziki metallov*, 13 (1), 71–100.
14. Shkoda, N. H., Shostak, S. V., Kryvoruchko, Ya. S. (2012). Interaction of electromagnetic radiation and nanocoatings. *Eastern-European Journal of Enterprise Technologies*, 6 (5 (60)), 8–12. Available at: <http://journals.uran.ua/eejet/article/view/5711/5156>
15. Hnuchi, Yu. B., Lerman, L. B., Shostak, S. V., Stetsenko, S. V. (2013). Pohlyannia elektromahnitnoho vyprominiuvannia bavhatosharovym kulovym chastyinkamy. *Machinery and Energetics*, 184, 142–149. Available at: <http://journals.nubip.edu.ua/index.php/Tekhnika/article/view/1242/1196>
16. Martynenko, I. I., Nikiforova, L. E. (2007). Innovatsionnaya tekhnologiya nizkoenergeticheskoy elektromagnitnoy obrabotki semyan. *Energetika, ekonomika, tekhnologiya, ekologiya*, 1, 89–92.
17. Li, J., Xu, Z., Zhou, Y. (2008). Theoretic model and computer simulation of separating mixture metal particles from waste printed circuit board by electrostatic separator. *Journal of Hazardous Materials*, 153 (3), 1308–1313. doi: <https://doi.org/10.1016/j.jhazmat.2007.09.089>
18. Pelevin, A. E. (2018). Magnetic and electrical enrichment methods. *Magnetic enrichment methods*. Yekaterinburg: Izd-vo UGGU, 296.
19. Kozyrskiy, V. V., Savchenko, V. V., Sinyavskiy, A. Y. (2019). Pre-Sowing Treatment of Leguminous Crop Seeds with a Magnetic Field. *Agricultural Machinery and Technologies*, 13 (1), 21–26. doi: <https://doi.org/10.22314/2073-7599-2018-13-1-21-26>
20. Mach, F., Kus, P., Karban, P., Doležel, I. (2012). Higher-Order Modeling of Electrostatic Separator of Plastic Particles. *Przegląd elektrotechniczny*, 12b, 74–76.
21. Kim, B., Han, O., Jeon, H., Baek, S., & Park, C. (2017). Trajectory Analysis of Copper and Glass Particles in Electrostatic Separation for the Recycling of ASR. *Metals*, 7 (10), 434. doi: <https://doi.org/10.3390/met7100434>
22. Nazarenko, I. (2013). Theoretical researches of co-operation of electric paul with dielectric suspension in systems of multielec-trodes. *Pratsi Tavriyskoho derzhavnoho ahrotehnolohichnoho universytetu*, 2 (13), 75–82.
23. Ciosk, K. (2012). Magnetic field and forces in a magnetic separator gap. *Przegląd elektrotechniczny*, 12b, 47–49.
24. Tarushkin, V. I. (2012). A mathematical model for improving dielectric separation devices. *Bulletin of Moscow State Agrarian University named V. P. Goryachkina*, 2, 7–9.
25. Prachukowska, A., Nowicki, M., Korobiichuk, I., Shewchyk, R., Salah, J. (2015). Modeling and validation of magnetic field distribution of permanent magnets. *Eastern-European Journal of Enterprise Technologies*, 6 (5 (78)), 4–11. doi: <https://doi.org/10.15587/1729-4061.2015.55323>
26. Volchenskov, V. I., Sobolev, V. A. (2013). On the features of modeling the magnetic circuit of a synchronous generator with per-

- manent magnets. Engineering Bulletin, MGTU im. Baumana, 9, 635–644.
27. Blank, A. V. (2004). Analytical calculation of the excitation field of a synchronous machine based on one piecewise-continuous eigenfunction. Sbornik nauchnykh trudov NGTU, 4 (38), 3–8.
28. Meessen, K. J., Gysen, B., Paulides, J., Lomonova, E. A. (2008). Halbach Permanent Magnet Shape Selection for Slotless Tubular Actuators. IEEE Transactions on Magnetics, 44 (11), 4305–4308. doi: <https://doi.org/10.1109/tmag.2008.2001536>
29. Afonin, A. A. (2005). Elektromagnitnye nagruzki elektricheskikh mashin s postoyannymi magnitami. Tekhnichna elektrodynamika, 1, 39–46.
30. Grinberg, G. A. (1948). Izbrannye voprosy matematicheskoy teorii elektricheskikh i magnitnyh yavleniy. Moscow-Leningrad: Izd. AN SSSR, 733.
31. Mirolyubov, N. N., Kostenko, M. V. et. al. (1963). Metody rascheta elektrostaticeskikh poley. Moscow: Vysshaya shkola, 415.
32. Sil'vester, P., Ferrari, R. (1986). Metod konechnyh elementov dlya radioinzhenerov i inzhenerov-elektrikov. Moscow: Mir, 229.
33. Zhang, Y. H., Xu, Y. Y., Ye, C. Y., Sheng, C., Sun, J., Wang, G. et. al. (2018). Relevance of electrical current distribution to the forced flow and grain refinement in solidified Al-Si hypoeutectic alloy. Scientific Reports, 8 (1). doi: <https://doi.org/10.1038/s41598-018-21709-y>
34. Tozoni, O. V. (1975). Metod vtorichnyh istochnikov v elektrotekhnike. Moscow: Energiya, 296.
35. Tihonov, A. N., Samarskiy, A. A. (1977). Uravneniya matematicheskoy fiziki. Moscow: Nauka, 735.
36. Verlan', A. F., Sizikov, V. S. (1978). Metody resheniya integral'nyh uravneniy s programmami dlya EVM. Kyiv: Naukova dumka, 219.
37. Tihonov, A. N., Arsenin, V. Ya. (1979). Metody resheniya nekorrektnyh zadach. Moscow: Nauka, 288.
38. Zaporozhets, Y., Ivanov, A., Kondratenko, Y. (2019). Geometrical Platform of Big Database Computing for Modeling of Complex Physical Phenomena in Electric Current Treatment of Liquid Metals. Data, 4 (4), 136. doi: <https://doi.org/10.3390/data4040136>
39. Govorkov, V. A. (1968). Elektricheskie i magnitnye polya. Moscow: Energiya, 488.
40. Tamm, I. E. (1976). Osnovy teorii elektrichestva. Moscow: Nauka, 616.
41. Polivanov, K. M. (1969). Teoreticheskie osnovy elektrotehniki. Ch. III. Teoriya elektromagnitnogo polya. Moscow: «Energiya», 352.
42. Pavlovskyi, M. A. (2002). Teoretychna mekhanika. Kyiv: Tekhnika, 512.