

## ABSTRACT AND REFERENCES

## APPLIED MECHANICS

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**DETERMINING THE CHARACTERISTICS OF VISCOUS FRICTION IN THE SLIDING SUPPORTS USING THE METHOD OF PENDULUM (p. 4-10)****Aleksandr Dykha**Khmelnitskyi National University, Khmelnytskyi, Ukraine  
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We analyzed the methods of determining the characteristics of friction based on the experimental studies using the damped oscillations of a pendulum. It was established that the available studies into characteristics of viscous friction lack the analytical description of the process of damped oscillations at viscous resistance and recommendations regarding practical calculation of the characteristics of friction. Here we propose a theoretical model of the swinging pendulum in the cylindrical sliding supports with a lubricant. It is demonstrated that for a pendulum in the lubricated sliding supports, the process of oscillations is described by a second order differential equation with viscous resistance, proportional to the deflection velocity of the pendulum.

It is found based on the solution of the equation that the ratio of adjacent amplitudes of damped oscillations is a constant magnitude, hence it follows that the absorption coefficient is constant over the entire process. We established, based on the theoretical model of pendulum oscillations, that for the viscous friction the absorption coefficient is equal to the doubled logarithmic damping decrement and is determined by one or a cycle of oscillations. The formulas are received for calculating the indicator of dynamic viscosity of a lubricant in the contact by the decrement of pendulum oscillations damping. The developed procedures for determining the characteristics of viscous friction are applied to examine the contact- viscous properties of different combinations of lubricating and design materials. The results received are aimed at searching for design and technological solutions in order to reduce the energy losses to friction in the sliding supports of machines.

**Keywords:** sliding support, method of pendulum, damped oscillations, absorption coefficient, oil viscosity.

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**DEVELOPMENT OF A DYNAMIC MODEL OF TRANSIENTS IN MECHANICAL SYSTEMS USING ARGUMENT-FUNCTIONS (p. 11-22)****Valery Chigirinsky**Zaporizhzhya National Technical  
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There are a number of applied problems in which it is necessary to take into account the dynamic component of the process or phenomenon including the fact that the load is applied not instantaneously but in time. For example, in continuous rolling, such combinations of mechanical systems appear in which action transfer from one rolling stand to another via the strip proceeds with some delay affecting transient processes and the strip gripping capability in the

adjacent stands of the continuous mill. The strip between the mill stands is in an elastic state. When the rolls start acting on it during the bite in the next stand, they transfer disturbance to the strip in a form of oscillations or in a form of a stationary action.

The aim of this research was to expand the application field of the obtained solutions to satisfy boundary and initial conditions formulated by applied production problems. The wave problem was considered as the process of propagation of the initial deviation and initial velocity.

On the basis of the method, the essence of which is the use of argument-functions, solution of dynamic linear and spatial problems of the elasticity theory was shown. In the course of the study, conditions for existence of new solutions for the wave problem, which are limited by the boundary conditions of various processes were shown. The initial differential equations and boundary conditions determine the type of differential equations for the argument-functions that close the solution. Argument-functions can be restricted by the Cauchy-Riemann relations and the corresponding differential invariants on the one hand and the differential relationships which result in that the argument-functions are the same for adjacent coordinate-time dependencies on the other hand. Besides, analytical dependences on the parameters entering into the d'Alembert formula were obtained.

**Keywords:** dynamic problem, wave equation, flat functions, adjacent stands, argument-functions, conditions for the existence of solutions.

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#### METHODS OF BALANCING OF AN AXISYMMETRIC FLEXIBLE ROTOR BY PASSIVE AUTO-BALANCERS (p. 22-27)

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The conditions for the occurrence of auto-balancing when balancing a flexible axisymmetric rotor by any number of passive auto-balancers of any type are determined. The problem is actual for the high-speed rotors working at supercritical speeds (rotors of aircraft engines, gas turbine engines of power plants, etc.).

The empirical criterion for the occurrence of auto-balancing is applied. Transformations were carried out on the example of the flexible axisymmetric rotor of constant section on two rigid hinge supports. The findings are applicable to rotors with another type of fixing.

It is established that auto-balancing of the rotor by  $n$  passive auto-balancers located in different correction planes is possible only if the rotor speed exceeds the  $n$ -th critical speed. The number of auto-balancers can be arbitrary. Between the critical rotor speeds, additional critical speeds appear. Auto-balancing occurs whenever the rotor passes a critical speed and disappears whenever the rotor passes an additional critical speed.

If  $n$  auto-balancers are located in the  $n$  nodes of the rotor flexural  $(n+1)$ -th mode, the  $j$ -th additional critical rotor speed matches with the  $j(n+1)$ -th critical speed,  $/j=1, 2, 3, \dots/$ . When balancing the flexible rotor between the  $n$ -th and  $(n+1)$ -th critical speeds, such number and placement of auto-balancers are optimum. Auto-balancers at the same time balance the first  $n$  distributed modal unbalances and do not respond to the  $(n+1)$ -th ones.

The additional critical speeds are due to the installation of the auto-balancers on the rotor. Upon transition to them, the behavior of auto-balancers changes. At slightly lower rotor speeds, the auto-balancers reduce the rotor unbalance, and at slightly higher ones – increase it.

**Keywords:** flexible rotor, passive auto-balancer, auto-balancing, criterion for occurrence of auto-balancing, critical speeds of flexible rotor.

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### NUMERICAL STUDY OF FLOW IN THE STAGE OF AN AXIAL COMPRESSOR WITH DIFFERENT TOPOLOGY OF COMPUTATIONAL GRID (p. 28-33)

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We conducted a series of calculations with the models of turbulent viscosity  $k$ - $\epsilon$ , SST and three variants of three-dimensional unstructured computational grids. For each variant of the computational grid we calculated each of the two models of turbulent viscosity at axial velocity at input from 110 to 150 m/s. Comparison of results of numerical experiments with data of the physical experimental studies revealed that an error of the computational research is 0.3...8.6 %. Results of the study showed that at the first phase of calculation of the stage of an axial compressor one can recommend using the model of turbulent viscosity  $k$ - $\epsilon$  and the coarse computational grid. To solve the problems on internal aerodynamics of compressors taking into account the flow in the near-border layer and aerodynamic trail, it is expedient to employ the model of turbulent viscosity SST and the fine adaptive grid.

**Keywords:** simulation of flow, computational grid, model of turbulent viscosity, stage of compressor, near-border layer.

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**COMPUTER SIMULATION OF HYDRAULIC FLOW IN A MIXING DEVICE WITH A DIAPHRAGM OF SPECIAL DESIGN INSTALLED IN IT (p. 33-39)**

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The results of computer simulation of hydrodynamic flow were presented using the FlowVision software package (Moscow, Russian Federation). This program has enabled creation of hydrodynamic flow models using three types of mixers: a mixer with the proposed diaphragm of special design, a pipe mixer and an orifice mixer. The complete information on behavior of the processes was obtained taking into account design and technological parameters of the abovementioned types of mixers. Computer simulation of flow in mixers of various types made it possible to substantially shorten time for conducting studies and confirm the results of field experiments presented earlier by the authors [11].

As a result of the analysis of the data obtained in the computer simulation of motion of the flow of waste water with the reagent solution, the following can be distinguished: when using different types of mixers, the best results of intensive flow mixing were obtained by using a mixer with a diaphragm of a special design and an orifice mixer. It is evidenced by the diagrams of distribution of pressure and velocities in these mixers. However, when using an orifice mixer, one can notice intensive mixing only at the center of the flow, and zones were noticeable at the walls of the pipeline in which there was practically no vortex formation and mixing respectively. In the pipe mixer, only a small region could be noticed in an immediate vicinity of the point of injection of the coagulant solution. Pressure and velocity vary in this region but these parameters change insignificantly in the main flow. The obtained hydrodynamic models indicate that the proposed diaphragm of a special design provides more efficient mixing of wastewater with the reagent. Models for pipe and orifice mixers have shown worse results. The proposed diaphragm enabled mixing of wastewater with the reagent as fully and quickly as possible.

**Keywords:** static mixer, computer simulation, pressure and velocity distribution diagram, turbulent dissipation.

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**FORMALIZATION OF DESIGN FOR PHYSICAL MODEL OF THE AZIMUTH THRUSTER WITH TWO DEGREES OF FREEDOM BY COMPUTATIONAL FLUID DYNAMICS METHODS (p. 40-49)**

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Based on theoretical and practical studies into the causes of losses of propellers, caused by the axial inflows, employing the methods of computational fluid dynamics, we calculated the geometry of physical model of the thrusters with two degrees of freedom. We specified the required physical conditions of implementation, formalized geometric parameters of the model, assigned the initial and boundary conditions of differential equations that describe behavior of propeller flows in the recirculation zones. The coefficients are calculated that take into account the existence of degradation effects.

The use of methods of computational fluid dynamics is necessary to account for the losses of propellers caused by the axial water inflows that are dependent on the degradation effects, which will contribute to reducing the propeller thrust and torque.

As the result of the studies, we received the Reynolds and Froude numbers for the zero-velocity model of the ship:  $R_n=4.405 \times 106$ ;  $F_r=3.124$ . Components of the axial and tangential forces of the radial distribution of steering propellers thrusts are refined within the limits of 2.7–5.1 %. The largest deviation of similarity coefficients is in the region of 85–100 % of the rated propeller thrust. We obtained dependences of adjustment factors that affect the components of thrusts and torques proportional to the radius of propeller of the model and the actual steering propeller, related to the original geometry. The value of correc-

tive factors depending on the propeller flow direction relative to the plane of motion of the ship is within the few hundredths of the percent. We systematized and compiled in the table the list of parameters (factors) according to the operating mode of the ship, which are required to solve the basic equations in the formalization of physical models of thrusters.

The designed principles of formalization of the physical models of thrusters could be employed in the process of selection and improvement of design of combined propulsive complex and adjustment of selected regulators of components of the ship power plant.

**Keywords:** ship steering propeller, degradation effect, formalization of the physical model, computational fluid dynamics.

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**PARAMETER OPTIMIZATION OF THE CENTRIFUGAL JUICER WITH THE BALL AUTO-BALANCER UNDER THE IMPULSE CHANGE OF AN UNBALANCE BY 3D MODELING (p. 50-58)**

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The optimization of the parameters of the centrifugal juicer with the ball auto-balancer under the impulse change of the sieve unbalance at cruising velocity is conducted by 3D modeling. The dependence of the duration of the transition processes on the main parameters of the juicer and the auto-balancer is studied.

Using the example of a two-ball auto-balancer, the impulse changes of an unbalance, which are the most unfavorable for the duration of transition processes, are found: the turn of the unbalance vector around the rotation axis of the rotor by 90° or 180°. In this, the balls pass the longest distance along the running track.

The following is established.

1. The proposed in previous works methods of optimizing the parameters of machines with an auto-balancer for minimization of the duration of transition processes are also efficient under the impulse change of an unbalance at cruising velocity.

2. The previously obtained results are confirmed, namely:

a) the increase of the number of the balls in the auto-balancer leads to the decrease of the duration of transition process; this is explained by the fact, that:

– when there are more than two balls in the auto-balancer, the multi-parameter family of the steady motions appears in the rotor machine;

– under the change of an unbalance, the balls make the transition between the two nearest steady motions;

b) the decrease of the running track radius leads to the decrease of the duration of transition processes; this is due to the fact, that the running track becomes more filled and the balls need to move less between auto-balancing positions;

c) the dependence of the optimal values of the parameters of the centrifugal juicer and the auto-balancer on the magnitude of an unbalance is revealed. The dependence is significant only for the two-ball auto-balancer and weakens with the increase of the number of the balls in the auto-balancer;

d) the use of the two-ball auto-balancer, both in practice and for theoretical and experimental studies of the duration of transition processes in auto-balancing of machines, is inexpedient.

3. It is established that at the centrifugal juicer run-up with the fixed unbalance and under the impulse change of its unbalance at cruising velocity:

– the trends in the influence of the running track radius of an auto-balancer and the number of the balls on the duration of transition processes are identical;

– the optimal values of the main parameters of the auto-balancer and the centrifugal juicer coincide, except for the coefficient of viscous resistance forces of the relative motion of the balls;

– the optimal values of the coefficient of viscous resistance forces of the relative motion of the balls at run-up are less than the corresponding values under the impulse change of an unbalance by 50 %.

**Keywords:** unbalance, auto-balancer, 3D modeling, impulse change of an unbalance, transition processes, centrifugal juicer.

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#### ANALYTICAL METHOD OF EXAMINING THE CURVILINEAR MOTION OF A FOUR-WHEELED VEHICLE (p. 59-65)

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We obtained equations for the curvilinear trajectory of a four-wheeled vehicle in the parametric form of a function of turning angle of the machine frame. The equations are suitable for the sections of entering a turn and exiting a turn. The proposed equations make it possible to build the trajectories taking into account the intensity of turning the front steered wheels. For this purpose, the course angle is represented as a function of the turning angle of the body of a machine. For example, in the case of a linear dependence, the proportionality factor (coefficient of intensity of change in the course angle, predetermined by the rotation speed of steered wheels) depends on the turning angle of a steering wheel. The solution was found based on the projections of velocity of the center of mass of a machine onto the inertial coordinate axes. In this case, the integrand functions are represented through a single variable – turning angle of the machine frame. For this purpose, we employed a special substitution, which replaces the differential of time with the differential of turning angle of the machine frame. Following the decomposition of integrand functions into the Maclaurin series, the integration becomes possible. We also found the equation of motion along a circular trajectory at fixed position of a steering wheel. Along with the equations for entering a turn and exiting a turn, they allow us to build complex trajectories of u-turns in a unified coordinate system. For the conjugation of separate sections of the trajectory, we applied formulas of change in the coordinates at parallel carry and turn of the coordinate axes. The coordinates of points along the trajectory can be calculated by using the software tools.

The impact of the phenomenon of wheels slip under the action of lateral forces on the trajectory of curvilinear motion is accounted for by introducing to the equations the intensity coefficients that represent dependence of the course angle, caused by the slip, on the turning angle of the machine frame.

**Keywords:** four-wheeled vehicle, curvilinear motion, equation of trajectory, course angle, lateral slip.

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